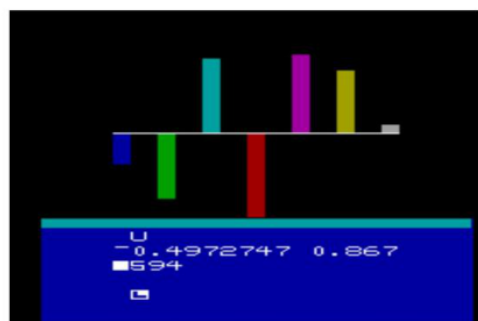




21 APL/S Games for Your Umtech VideoBrain

by James Price

21 APL/S Games and One-Liners for Your Umtech VideoBrain

APL Games for Microcomputers, Volume 1

James Price

Published by James Price, 2025.

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21 APL/S GAMES AND ONE-LINERS FOR YOUR UMTECH
VIDEOBRAIN

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All programs contained herein are original works by the author unless otherwise indicated. Programs are written in APL/S for compatibility with the Umtech VideoBrain. No original Umtech software, firmware, ROM code, source code, or proprietary documentation is reproduced, distributed, or derived. Any trademarks or product names referenced are used solely for identification and compatibility purposes and remain the property of their respective owners. While every precaution has been taken in the preparation of this book, the publisher assumes no responsibility for errors or omissions, or for damages resulting from the use of the information contained herein.

Acknowledgments

Thanks to Sean Riddle for making this all possible by performing the heavy lifting and technical magic needed to resurrect the APL/S ROMs so we can emulate The Computational Language of the Umtech VideoBrain using MAME. Thanks also to the APL/S cartridge donor, those on the MAME team who added the VideoBrain computer system to MAME, and the VideoBrain enthusiast community for keeping this system in their hearts all these years.

Thanks to The Array Cast team of Bob Therriault, Conor Hoekstra, Marshall Lochbaum, Adám Brudzewsky, and Stephen Taylor for having me on the show and encouraging me to push forward with writing APL games books. Thanks also to Marshall Lochbaum for his enthusiasm in documenting APL/S on the APL Wiki, and for hosting the Discord APL Farm “Quad Squad,” a weekly discussion of ACM SIGAPL Quote Quad articles, which lead to the port of the Unit Circle program.

Thanks to Elias Mårtenson for his encouragement and interest in this project and suggestions for improvements to the upcoming print edition.

Dedication

To my beloved tabby cat, Mr. Tibbs.

Thanks for hanging out with me while I was writing these games during late Summer and Autumn of 2025, little buddy.

Series Introduction

An early APL gaming culture left behind a rich treasure trove of artifacts now readily accessible to code archaeologists. Early issues of *Quote Quad* contained APL implementations of [Poker](#), [Target](#), [Conway's Game of Life](#), and [Tic Tac Toe](#). A game called [Pico-Fumi](#) is found in the *Proceedings of the Fifth International APL Users' Conference* (May 1973). Gaming historians digging through program listings on [MTS](#) systems running on IBM System/360s will uncover a [resource management game](#) called [Kingdom](#) written in APL. An issue of the I. P. Sharp newsletter called for submissions of [WARI](#) (Mancala) playing programs. The submitted entries then fought a series of battles, and the winners were reported in a [follow-up issue](#).

I.P. Sharp newsletters from the late 1970's document a [91 FUNSPACE](#) workspace, and track the evolution of 92 GAMES, which included [ELIZA](#), [STARTREK](#), [SPACEWAR](#), [GAMBLE](#), [SNIM](#), [WARGAMES](#), [WORDGAMES](#), [MASTERMIND](#), [QUADGT](#), [WUMPUSHUNT](#), and a game called "Bridge Hands".

The I.P. Sharp [Public Workspaces Catalogue](#) entry for 92 GAMES from 1981 lists "tictactoe, blackjack, showdown poker, slot machine, craps, horserace, supernim, gunfire games, hangman, scramble, and finite-state machine, nim, mastermind, wumpus, and quadgit." It also includes 93 LIFE: "[This workspace contains Life, a solitaire game involving a world in which cells live and die according to a few simple rules. The rules have been chosen to make the behaviour of the cell population quite interesting.](#)"

The MCM/70's APL library [LIB/70](#) included a "[Fun and Games Library](#)" in 1974 consisting of "[several games, such as HOR \(HORSE, possibly the world's earliest game implemented on a microcomputer\), HAN \(HANGMAN\), GUN, etc.](#)" Reviewing the tape, one also finds the source code to games like [Moo](#), [Craps](#), and [Blackjack](#).

Back then, it was common to [type in](#) programs from print media. A [Lunar Lander](#) game appears in the APL-themed August 1977 issue of *Byte* magazine, immediately following Ken Iverson's article "Understanding APL." Type-in programs were published in

magazines, like Creative Computing and [Compute's Gazette](#), and in books of games written in BASIC by authors like [David Ahl](#) and [Tim Hartnell](#). BASIC was built into the microcomputers used in schools, Apple IIs and Commodore PETs, and in homes, Timex/Sinclair 1000s, Commodore 64s, and Atari 800XLs.

David Ahl explained in an [interview](#): “BASIC was the only widely available interactive language. Smalltalk? Lisp? Logo? MUMPS? They didn't stand a chance against BASIC.” Steve Wozniak recalls his motivation for writing Integer BASIC for the Apple computer: “There was a book out, 101 BASIC Computer Games, and Bill Gates had written in BASIC. So I said: [You've got to have these games; it's going to be the heart of a computer that's worth anything to people...](#)”

But with BASIC everywhere, many critics lamented the harm such a questionable language would inflict on vulnerable programming populations. Early use of BASIC was said to leave one “[mentally mutilated beyond hope of regeneration](#).” Did [learning such a poorly crafted tool of thought first](#) leave [malleable young minds](#) permanently [misshapen](#)? To what extent did the use of BASIC represent a lost opportunity to introduce the microcomputer generation to structured programming?

What if, by a twist of fate, instead of BASIC, APL had been the language built into home microcomputers? What if an APL workspace had greeted programmers instead of the BASIC prompt? Like BASIC, APL is interpreted and well-suited to writing games. The Waterloo APL disk for the Commodore SuperPET shipped with a version of MASTERMIND, and the APL/Z80 disk included an implementation of Conway's Game of Life.

So what might an APL games book have looked like, if APL had been the standard built-in language? These books explore APL in the spirit of learning the language by writing some of those games. This series will examine APL variants running on the Umtech VideoBrain, the Commodore SuperPET, the Commodore 64 and C128, and the MCM/70.

Introduction to APL/S on the Umtech VideoBrain running on MAME

The 1977 Umtech VideoBrain's programming language offering, The Computational Language cartridge, provided users with an interactive APL/S workspace with 920 bytes of free memory. All user programs and data, including variables and arrays, needed to fit into this tiny workspace. Numbers were stored as 4-byte floating points, with program keywords and variable references stored as single byte tokens.

Working within this very small workspace can be a challenge, especially when including visualization techniques provided by the primitive bar graph facility. Most of the games in this book use the bar graph feature in some way. Many of these games use almost every single byte of memory. Part of the fun in writing games for the VideoBrain is to see if you can squeeze in just one more feature, like adding leap year handling code to the clock calendar program. Sometimes a little space can be freed up by leaving initial variable assignments out of the program, and only typing them in before running it, or by shortening text strings used in output. The APL/S language is a good choice for code golfing.

Using MAME makes program development a lot easier, since you may save and load games using the debugger. The debugger can be used to examine memory and the stack. MAME even lets you speed up the system by skipping frames. You can remap keys, and I found the 'A' key needed to be remapped to the '.' key since the real 'A' key was inexplicably showing up as the 'O' key.

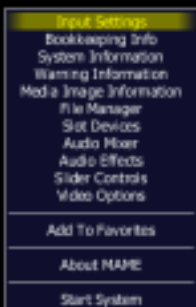
There are known problems with this system:

Imperfectly emulated features: sound

THIS SYSTEM DOESN'T WORK. The emulation for this system is not yet complete. There is nothing you can do to fix this problem except wait for the developers to improve the emulation.

Press any key to continue

If you also need to remap the 'A' key, here's how: first, when loading The Computational Language cart, hit the TAB key [here](#).



Input Settings

Input Assignments (this session)

Analog Input Adjustments
Keyboard SelectionInput Assignments (general)
Input Devices

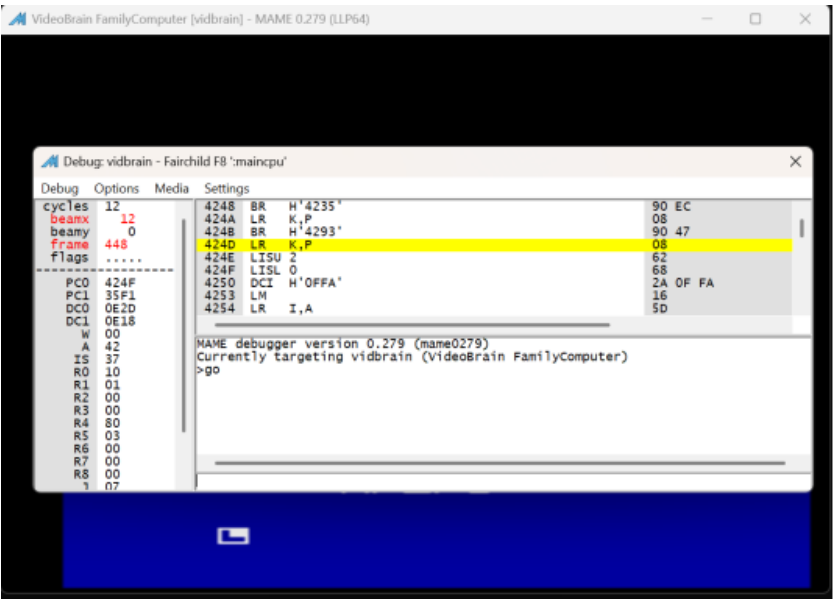
Return to Previous Menu

Input Assignments (this system)

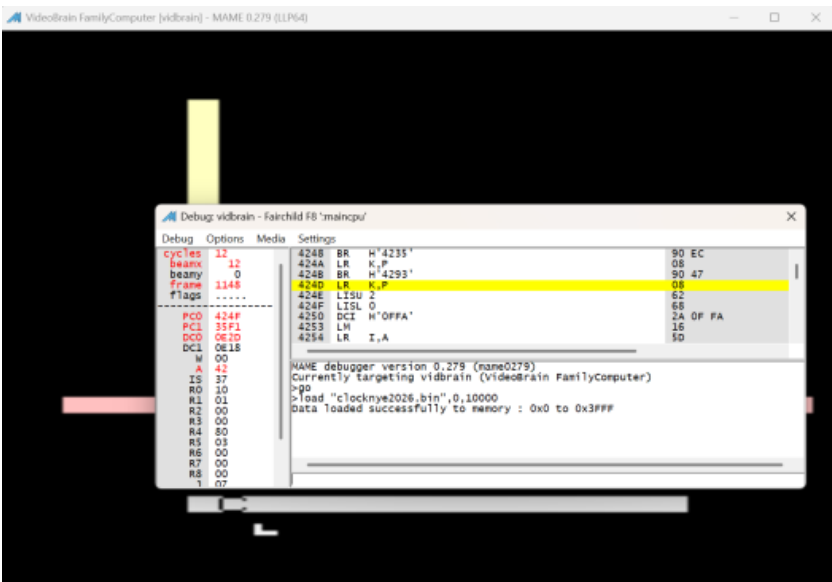
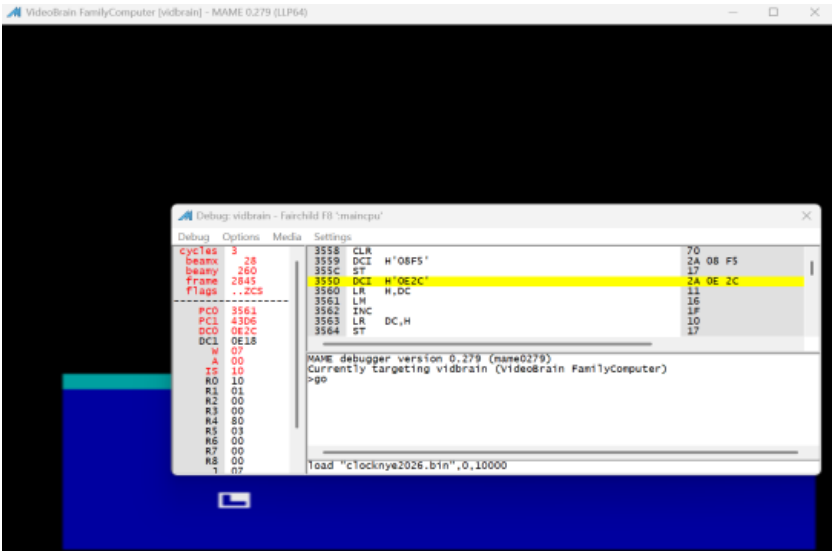
AD Stick X 4 Analog Dec	None
AD Stick Y 4 Analog	n/a
AD Stick Y 4 Analog Inc	None
AD Stick Y 4 Analog Dec	None
ERASE RESTART	Kbd Backspace
SPACE RUN/STOP	Kbd Space
' *	Kbd ,
; n	Kbd ;
? 0	Kbd /
A .	Kbd A or Kbd .
B =	Kbd B
C 3	Kbd C
D 5	Kbd D
E 8	Kbd E
F 6	Kbd F
G -	Kbd G
H /	Kbd H
I *	Kbd I
J (	Kbd J
K)	Kbd K
L \$	Kbd L
M :	Kbd M
N ,	Kbd N
O #	Kbd O

Press Kbd Enter or Kbd Num Enter to set
Press Kbd Delete to clear

Then, go to the Input Settings for the keyboard keys, set the new ‘A’ key, and you’re good to go.



To load games in the debugger, launch MAME with the -debug option (you can also use the -window option to run MAME in a window). When the debugger starts up, type ‘go’ and hit return.



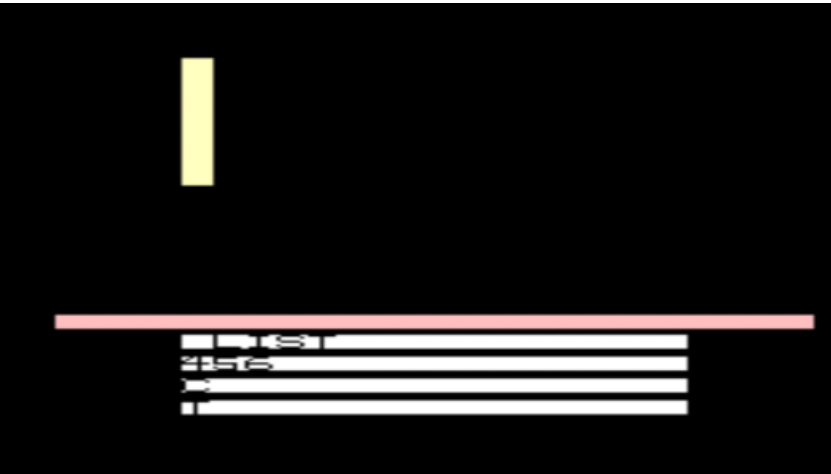
Now load a game by typing “load GAME.bin,0,10000” where GAME is the game name. Games are similarly stored by typing “save GAME.bin,0,10000” in the debugger. Click the debugger closed (it can be re-opened with the ‘ key).



The game is now loaded, and ready to run. Hit the F3 key to execute the program.

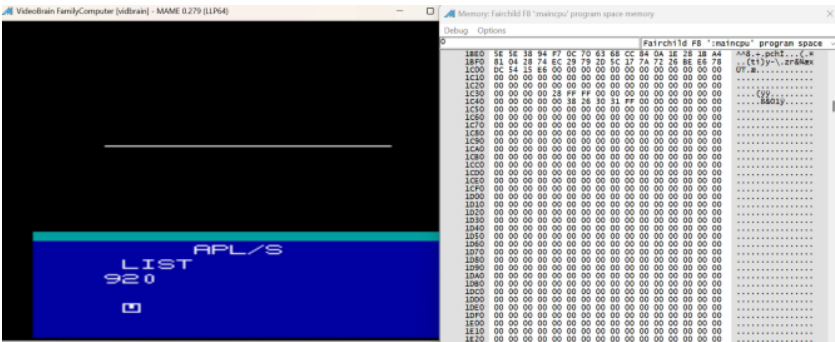


The program starts to run. The screen will look a little different than it usually looks after loading in a program using the debugger.

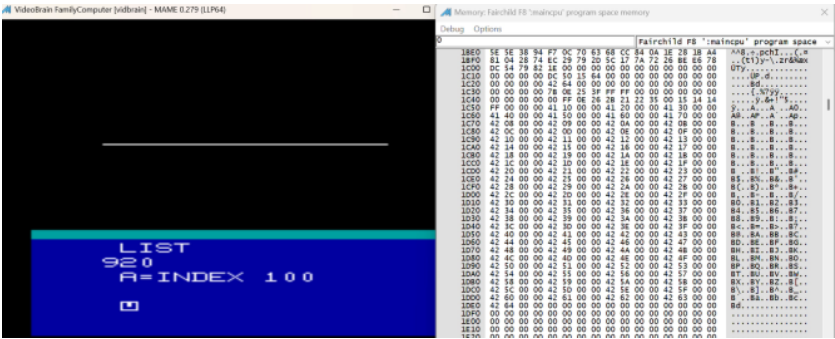


Alternatively, instead of running the program, you can LIST the variables and programs. Hit F1 to use the backspace to remove the program name, 'C', and then type LIST and hit F3 to enter the command.

LIST causes the free space remaining in the workspace to be shown, followed by the names of all programs and variables used.



The debugger can easily be used to examine programs and variables in memory. Click on Debug, then select New Memory Window to open a window to view the system memory.



We quickly fill up 400 bytes of the 920 bytes of free memory by creating an array of 100 numbers.

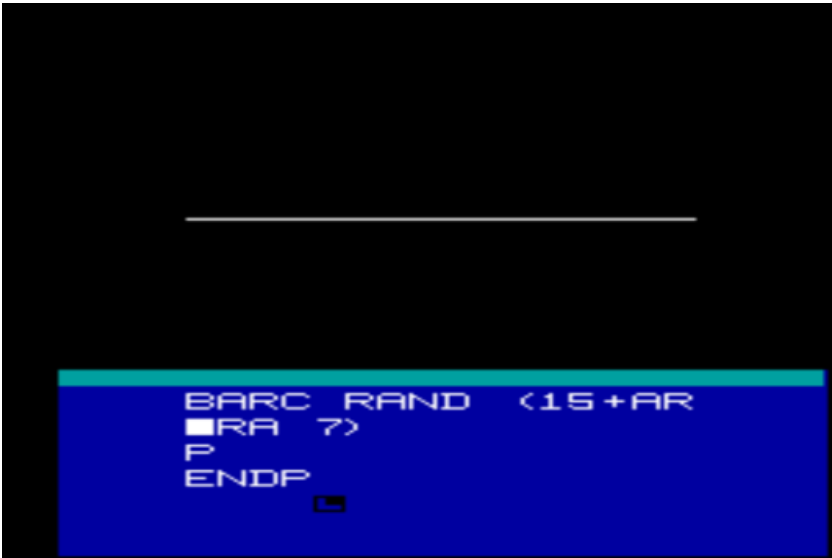
Watching the memory window during program runs can be very entertaining and offers insights into the operation of the system. We'll examine the stack operation in the Recursive Factorial Fun program chapter.

As far as I can tell, you cannot run the debug mode and use frame skipping at the same time. To speed up the system, run MAME without the debug flag, then increase system speed using frame skipping as usual. The only drawback seems to be that one cannot speed up a game loaded in using the debugger.

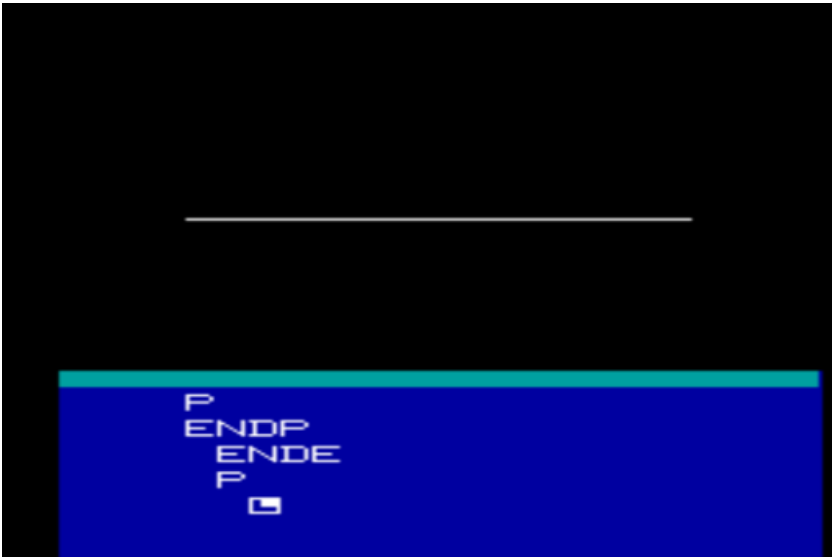
```
EDIT P
PROG P
BARH RAND (64+A
■RRA 7)
```



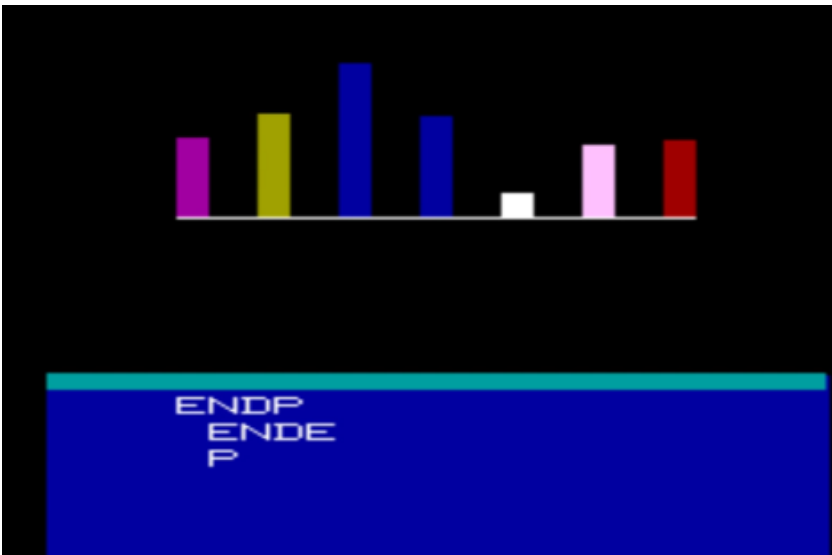
To enter in a new program, type EDIT PROGNAME, for example, EDIT P.



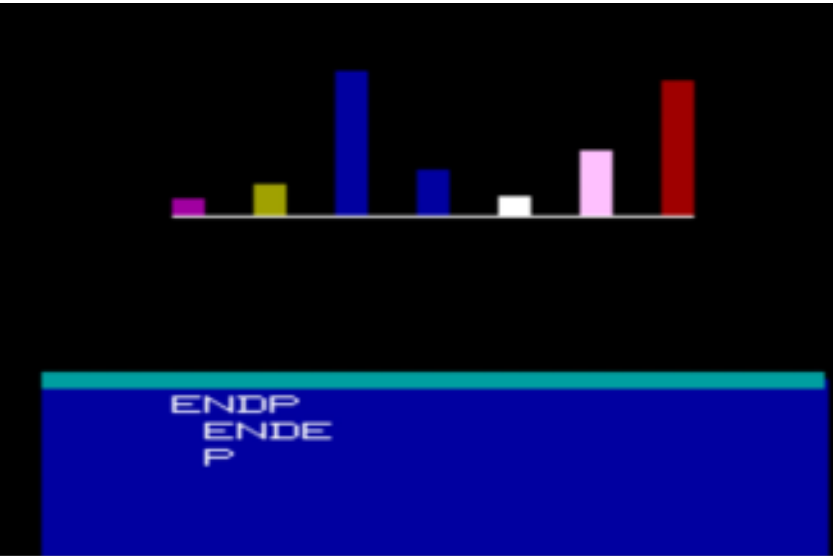
End the program with ENDP.



Type ENDE to exit the program editor. Then run the program by typing 'P' and hitting F3. (F2 moves the editor back one line, and F4 opens a new line in an existing program.)

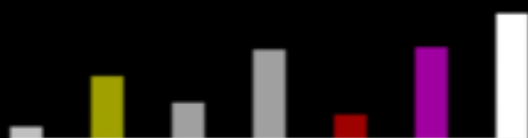


The program generates bar graphs of random height and color, then calls itself recursively.

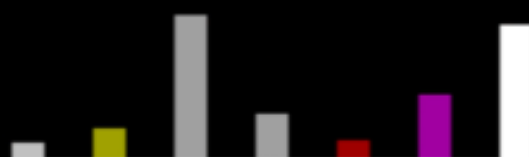




ENDP
ENDE
P



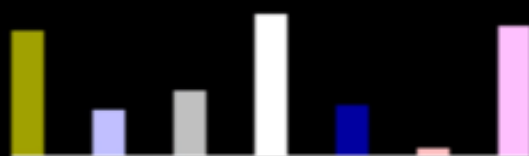
ENDP
ENDE
P



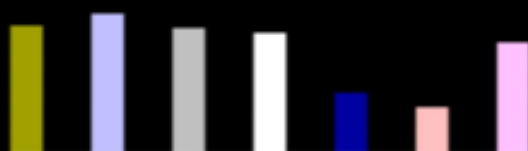
ENDP
ENDE
P



ENDP
ENDE
P



ENDP
ENDE
P



ENDP
ENDE
P



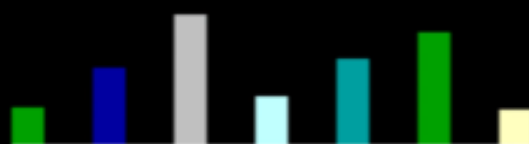
ENDP
ENDE
P



ENDP
ENDE
P



ENDP
ENDE
P



ENDP
ENDE
P

That should be enough information to get you started. I hope you have fun experimenting with the system, playing these games, and writing your own programs!

Slot Machine

A simplified port of the [David Ahl Basic Computer Games SLOTS](#) game.

```

PROG SLOT
CASH=100
BARH 20 20 20
WHILE 1
DO CASH
"BET $1?"
IF 0 GE BET=KEYB
THEN EXIT
ENDIF
BARC RAND 6 6 6
BARC RAND 6 6 6
BARC RAND 6 6 6
BARC RAND 6 6 6
BARC RAND 6 6 6
BARC RAND 6 6 6
Z=RAND 6 6 6
BARC Z
I=+/ (Z(1) EQ Z)
IF I EQ 3
THEN
    "3 OF A KIND"
    CASH=CASH+5
ELSE
IF I EQ 2
THEN
    "2 OF A KIND"
    CASH=CASH+3
ELSE
    J=+/(Z(3) EQ Z)
    IF J EQ 2
    THEN
        "2 OF A KIND"
        CASH=CASH+3
    ENDIF
ENDIF
ENDIF
CASH=CASH-1
ENDWHILE
ENDP

```

SLOT MACHINE

Description

The slot machine on one-arm bandit is a mechanical device that will absorb coins just about as fast as you can feed it. After inserting coin, you pull a handle that sets three independent reels spinning. If the reels stop with certain symbols appearing in the pay line, you get a certain payoff. The original slot machine, called the Liberty Bell, was invented in 1895 by Charles Fey in San Francisco. Fey refused to sell or lease the manufacturing rights, so H.S. Mills in Chicago built a similar, but much improved, machine called the Operators Bell. This has survived nearly unchanged to today.

On the Operators Bell and other standard slot machines, there are 20 symbols on each wheel but they are not distributed evenly among the objects (cherries, bar, apples, etc.). Of the 8,300 possible combinations, the expected payoff (to the player) is 7,049 or \$89.11 for every \$100.00 put in, one of the lowest expected payoffs of all casino games.

In the program here, the payoff is considerably more liberal; indeed it favors the player by 11%—i.e., an expected payoff of \$111 for each \$100 bet. To approximate Nevada odds, reduce the jackpot to \$15 and keno to \$4.

Source

Lots of slot machine programs were submitted including a very nice one by Rob Hoffberg of Roslyn, NY. The author of the one published is unknown.

PROGRAM LISTING

[illegible]

1991 10 4 1991
Date Recd. 1991

[illegible]

PROGRAM LISTING

```

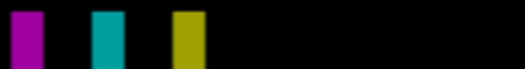
100 RANDOMIZE
110 DIM D(3)
120 PRINT"THIS IS A SIMULATION OF A SLOT MACHINE USING A COMPUTER "
130 PRINT "EACH TIME YOU 'PULL' I WILL ASK YOU IF YOU WISH TO PLAY AGAIN. "
140 PRINT "JUST ANSWER WITH A 'Y' FOR YES OR A 'N' FOR NO. "
150 PRINT "PLEASE PLACE 4 QUARTERS ON MY CPU FOR EACH PLAY. "
160 PRINT
170 FOR B1=1 TO 3
180 LET D(B1)=INT(RND(0)*6)+1
190 NEXT B1
200 FOR G1=1 TO 3
210 IF D(G1)=1 THEN 280
220 IF D(G1)=2 THEN 300
230 IF D(G1)=3 THEN 320
240 IF D(G1)=4 THEN 340
250 IF D(G1)=5 THEN 360
260 IF D(G1)=6 THEN 380
270 GOTO 580
280 PRINT TAB(G1*7); " BELL";
290 GOTO 390
300 PRINT TAB(G1*7); " BAR";
310 GOTO 390
320 PRINT TAB(G1*7); "CHERRY";
330 GOTO 390
340 PRINT TAB(G1*7); "APPLE";
350 GOTO 390
360 PRINT TAB(G1*7); "LEMON";
370 GOTO 390

```

SLOT
100
BET \$1?
?1
□



?1
99
BET \$1?
?1
☐



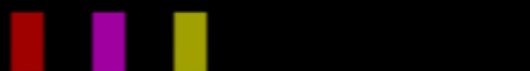
?1
98
BET \$1?
?1
☐



?1
97
BET \$1?
?1
□



?1
2 OF A KIND
99
BET \$1?



?1
98
BET \$1?
?1
□



?1
2 OF A KIND
100
BET \$1?



?1
99
BET \$1?
?1
□



?1
98
BET \$1?
?1
☐



?1
3 OF A KIND
103
BET \$1?



?1
102
BET \$1?
?1
□



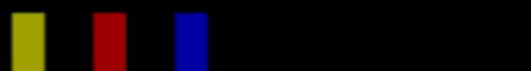
2 OF A KIND

104

BET \$1?

?1





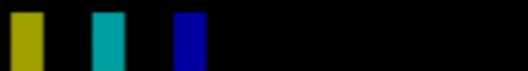
```
?1
103
BET $1?
?1
  □
```



2 OF A KIND
105
BET \$1?
?1
☐



?1
104
BET \$1?
?1
□



?1
103
BET \$1?
?1
□



2 OF A KIND
105
BET \$1?
?1
☐



?1
104
BET \$1?
?1
□



?1
2 OF A KIND
106
BET \$1?



?1
105
BET \$1?
?1
□



2 OF A KIND

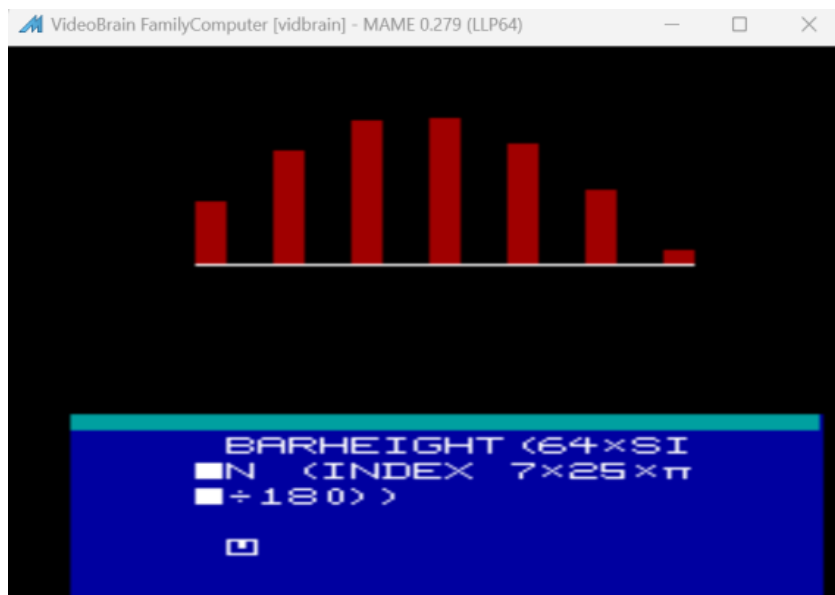
107

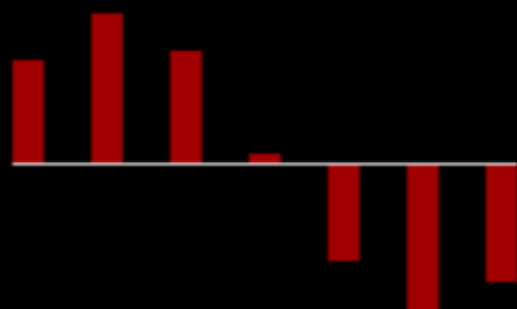
BET \$1?

?



Sine Barchart One-Liner





APL/S
BARH 64×SIN (IND
■E 7×22×π+90)

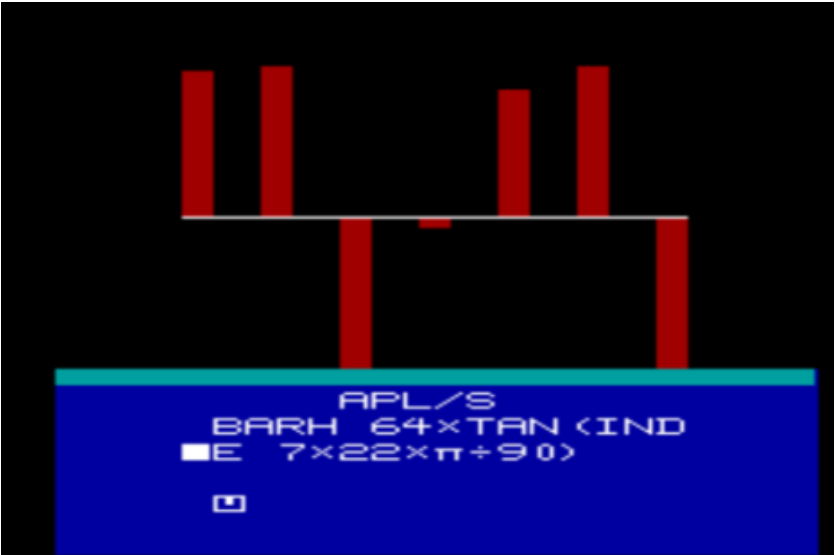




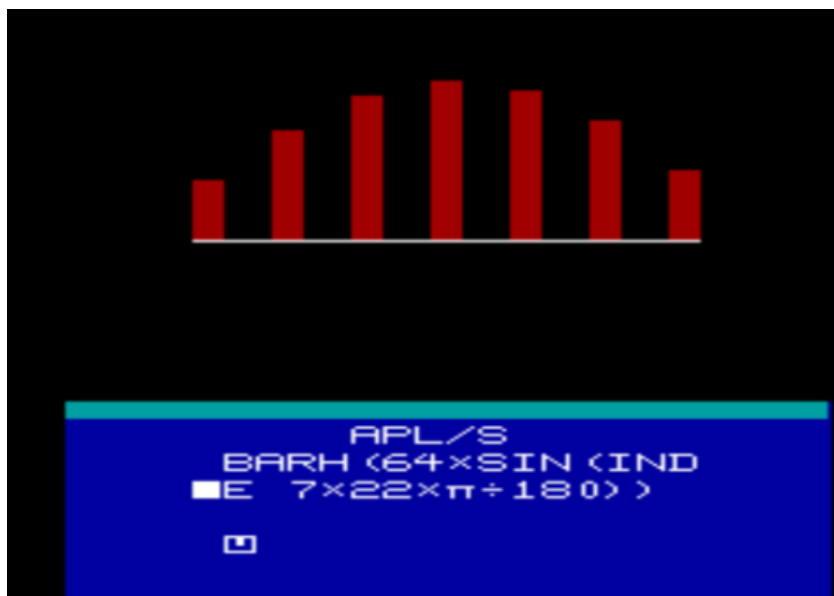
APL/S
BARH 64×COS (IND
■E 7×22×π+90)



Cosine bar charted similarly.



Tangent graphed at the same points.



Change the sine chart's pi divisor from 90 to 180 to focus only on the positive value portion.

```
APL/S
S=22×INDE 7
```



Let's walk through it, step by step.

```
S
22 44 66 88 110
■132 154
```



Sample the sine curve using 7 values between 0 and 180 degrees.



Now convert from degrees to radians by multiplying by pi and dividing by 180.

■ .303834 2.68780

■ 8

S=SIN S

□

```
S=SIN S
S
0.3746067 0.6946
```

Take the sine of each of the 7 values in the array.



Scale up to 64 since the bar chart holds values between -64 and 64.



After scaling.

■3	58.4669	63.96
■1	60.1403	47.56
■134	28.05571	





■ 1 60.1403 47.56
■ 134 28.05571
BARH S



Now chart the scaled values. They do not need to be integers.



■ 134 28.05571

BARH S

BARC INDE 7



Change colors with a simple BARC using INDEX 7.

Acey Ducey

A port of David Ahl's 1973 [ACEYDU](#) from "101 BASIC Computer Games"

```
PROG ACEY
BARC 3 4 3
N 100
```

```

PROG ACEY
BARC 3 4 3
N=100
Q=100
WHILE Q GT 0
DO
    "YOUR CASH"
    Q
    "YOUR CARDS"
    A=RAND 13 13 13
    WHILE A(1) GE A(3)
    DO
        A=RAND 13 13 13
    ENDW
    Z=A(1)
    CARD
    Z=A(3)
    CARD
    BARH 4.5x(A(1),0,A(3))
    "BET?"
    M=KEYB
    IF M EQ 99
    THEN EXIT
    ENDIF
    Z=A(2)
    CARD
    IF (Z GT A(1)) AND (Z LT A(3))
    THEN "YOU WIN"
        Q=Q+M
        BARC 3 2 3
    ELSE "YOU LOSE"
        Q=Q-M
        BARC 3 4 3
    ENDIF
    BARH 4.5xA
ENDW
ENDP

```

The Acey Ducey main program.


```
PROG CARD
IF (Z NE 1) AND (Z LT 11)
THEN Z
ELSE
  IF Z EQ 1
  THEN "ACE"
  ELSE
    IF Z EQ 11
    THEN "JACK"
    ELSE
      IF Z EQ 12
      THEN "QUEEN"
      ELSE "KING"
      ENDI
    ENDI
  ENDI
ENDI
ENDP
```

The main program calls the CARD subprogram to generate cards.



ACEY
YOUR CASH
100
YOUR CARDS

A sample game.



4
5
BET?
?1
□



?1
KING
YOU LOSE



YOUR CASH
99
YOUR CARDS



ACE
KING
BET?
?50





2
YOU WIN
YOUR CASH



149
YOUR CARDS
2
QUEEN



2
QUEEN
BET?
?100
□



7
YOU WIN
YOUR CASH



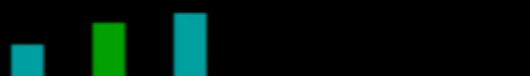
YOUR CASH
249
YOUR CARDS



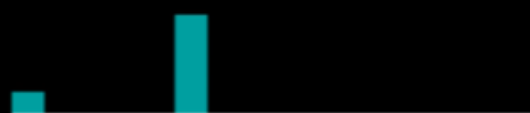
63
BET?
?1
□



?1
5
YOU WIN



YOUR CASH
25 0
YOUR CARDS



2
9
BET?
?4
□



2
YOU LOSE
YOUR CASH



246
YOUR CARDS
ACE
5



ACE
5
BET?
?5
0



3
YOU WIN
YOUR CASH



251
YOUR CARDS
5
7

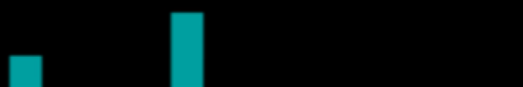


5
BET?
2

ACEY
YOUR CASH
100

Another sample game.





BET ?
?5
2



2
YOU LOSE
YOUR CASH
95



YOUR CARDS
2
KING



BET ?
?55
4



4
YOU WIN
YOUR CASH



150
YOUR CARDS
8



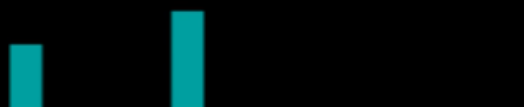
8
KING
BET?
5
C



?S
QUEEN
YOU WIN



YOUR CASH
155
YOUR CARDS



6
9
BET?
?
□

Roulette

First, enter the program. Then, before running, type:

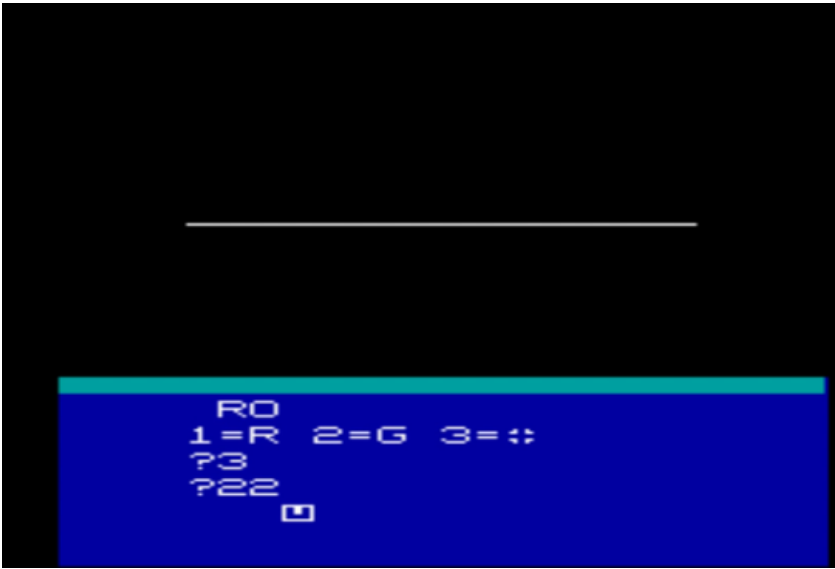
N=0

BARH 30

```

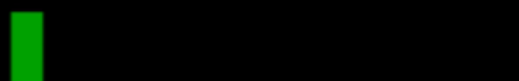
PROG R0
M=100
R=1 3 5 7 9 12 14 16 18 19 21 25 27 30 32 34 36
G=2 4 6 8 10 11 13 15 17 20 22 24 26 28 29 31 33 35
WHILE 1
DO
    M=M-1
    "1=R 2=G 3=#"
    P=KEYB
    IF P EQ 3
    THEN N=KEYB
        IF N EQ 99
        THEN EXIT
    ENDI
    ENDI
    S=RANDOM 37
    S=S-1
    S
    IF S EQ 0
    THEN BARC 8
        ELSE
            IF (+/(S EQ R))
            THEN BARC 4
            ELSE BARC 2
        ENDI
    ENDI
    IF (P EQ 3) AND (S EQ N)
    THEN "YOU WIN"
        M=M+35
        ELSE
            IF (P EQ 1) AND (+/(S EQ R))
            THEN "YOU WIN"
                M=M+2
            ELSE
                IF (P EQ 2) AND (+/(S EQ G))
                THEN "YOU WIN"
                    M=M+2
                ELSE "YOU LOSE"
            ENDI
        ENDI
    ENDI
    ENDI
    M
ENDW
ENDP

```



A sample game run.





99
1=R 2=G 3=::
?2



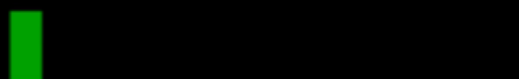
31
YOU WIN
100



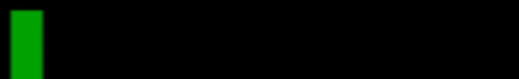
```
1=R 2=G 3=::  
?1  
21
```



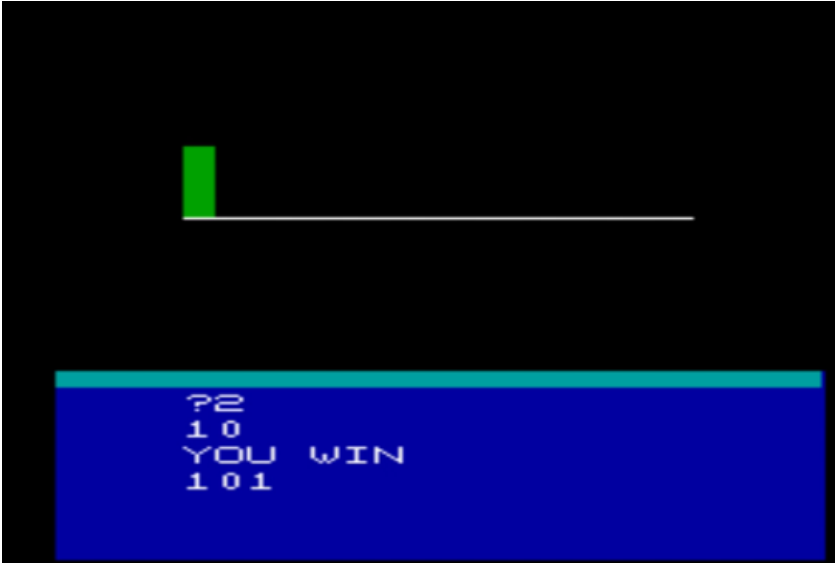
```
21  
YOU WIN  
101  
1=R 2=G 3=::
```

?1
20
YOU LOSE



YOU LOSE
100
1=R 2=G 3=::
?2
□

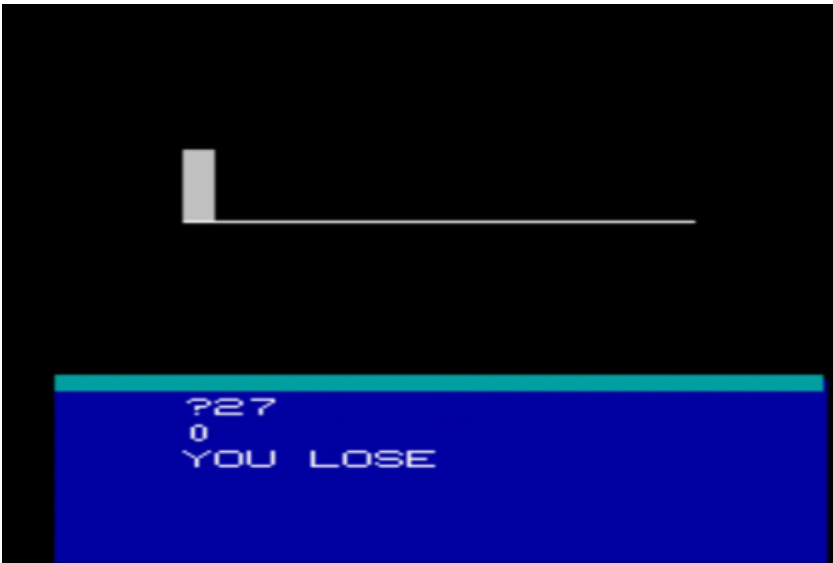
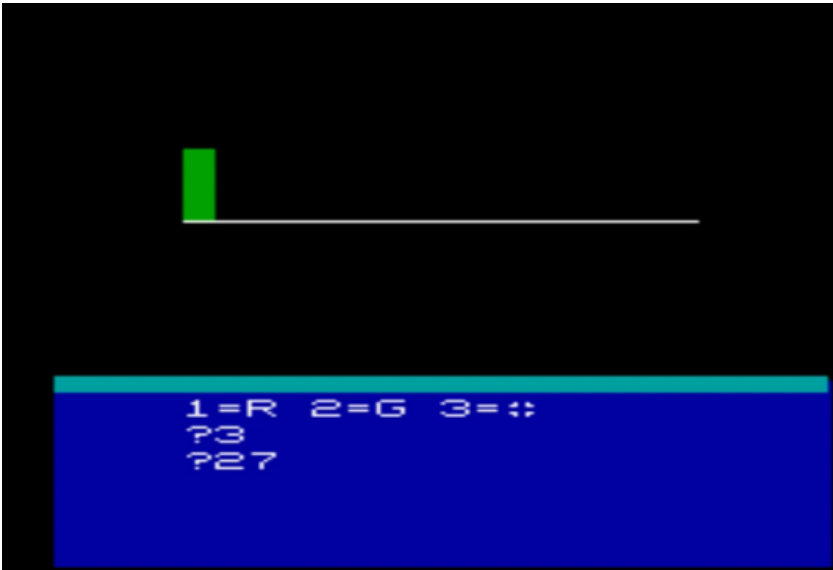


Exit the game by placing a wager on a roll of 99.



A big payout when the ball lands on the number the player wagered on.





The wheel rolls a 0. The house has the edge.

Gunner

A port of David Ahl's 1973 [GUNNER](#) from "101 BASIC Computer Games"

PROG GUN

7 6 61 0

```

PROG GUN
Z=S=S1=0
BARC 10
T=43000-RAND 30000
R=46500
"DISTANCE TO TARGET IS"
T
WHILE 1
DO
    "ELEVATION?"
    B=KEYB
    B2=2*(B÷57.3)
    I=R*(SIN B2)
    X=T-I
    E=FLOOR X
    IF ABS E LT 100
    THEN "YOU WIN"
    EXIT
    ENDI
    IF E GT 100
    THEN "TOO SHORT BY"
        BAR -30
    ELSE
        "TOO FAR BY"
        BAR 30
    ENDI
    ABS E
    S=S+1
    IF S EQ 6
    THEN "YOU LOSE"
    EXIT
    ENDI
ENDW
ENDP

```

GUN
DISTANCE TO TARG
■ET IS

■ET IS
13337
ELEVATION?
?13
□



TOO FAR BY
7046
ELEVATION?
?11





TOO FAR BY
4081
ELEVATION?
?7
□



TOO SHORT BY
2088
ELEVATION?
?8
□



TOO SHORT BY
520
ELEVATION?
?9





TOO FAR BY
1032
ELEVATION?
?8.5





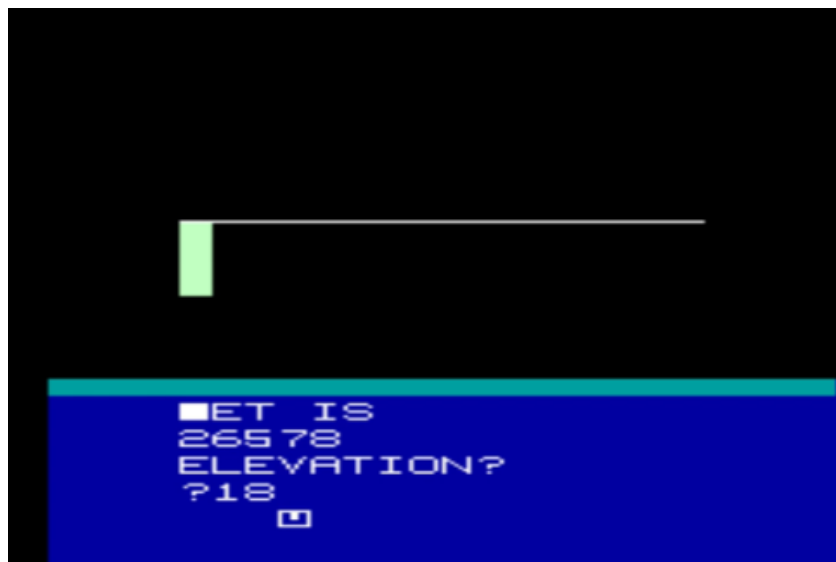
TOO FAR BY
258
YOU LOSE





GUN
DISTANCE TO TARG
■ET IS
26578

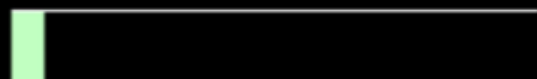
Another game.





TOO FAR BY
753
ELEVATION?
?17





TOO SHORT BY
577
ELEVATION?
?17.5





ELEVATION?
?17.5
YOU WIN



Collatz Bounce

The Collatz conjecture is a long-standing open question in mathematics built around an extremely simple process. Starting from any positive integer, a sequence is generated by repeatedly applying one of two rules: if the current value is even, it is divided by two; if it is odd, it is multiplied by three and increased by one.

Despite the simplicity of these operations, no proof exists that the process always ends the same way. The conjecture asserts that, regardless of the starting number, the sequence will eventually reach the value 1, after which it falls into a repeating cycle. This claim has been verified for vast ranges of integers, but a general proof, or a counterexample, remains unknown.

```
PROG COLLATZ
BARC 3
SCORE=0
"ENTER YOUR NUMBER TO COLLATZ BOUNCE"
NUM=I=KEYB
TOP=I
WHILE I NE 1
DO
    IF I MOD 2 EQ 0
    THEN I=I÷2
        BARH -30
    ELSE I=1+3×I
        BARH 30
    ENDI
    SCORE=SCORE+1
    I
    IF I GT TOP
    THEN TOP=I
    ENDI
ENDW
BARH 0
"NUM TOP SCORE"
NUM,TOP,SCORE
ENDP
```

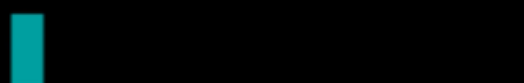
C
ENTER YOUR NUMBE
■R TO COLLATZ BO
■UNCE



■ UNCE
735
106



735
106
53

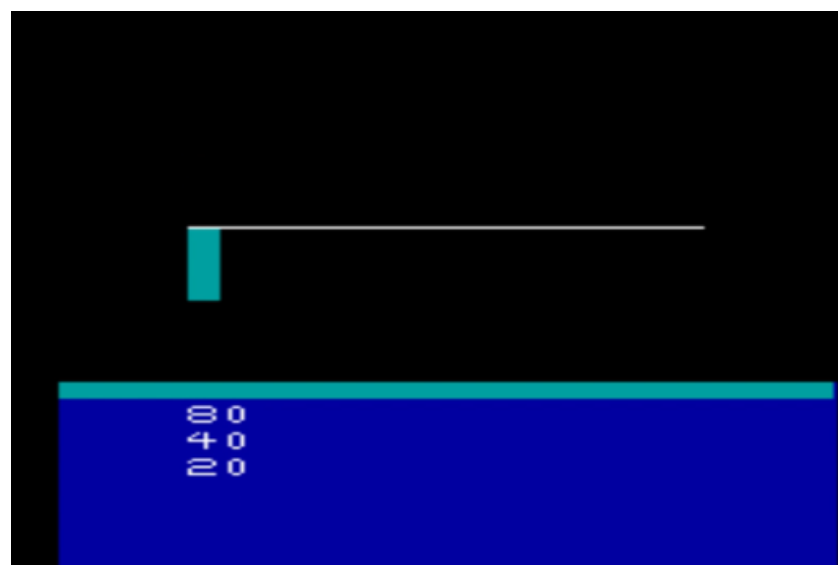


106
53
160



53
160
80

160
80
40





20
10
5

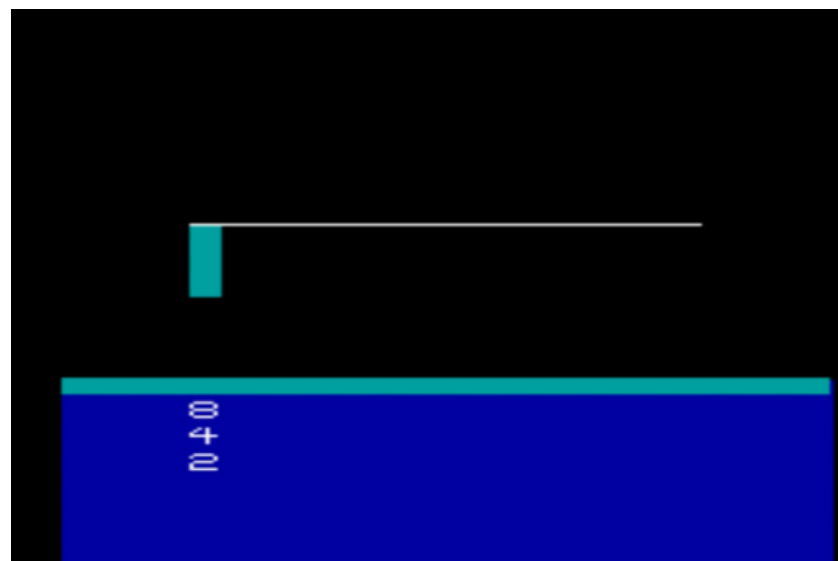


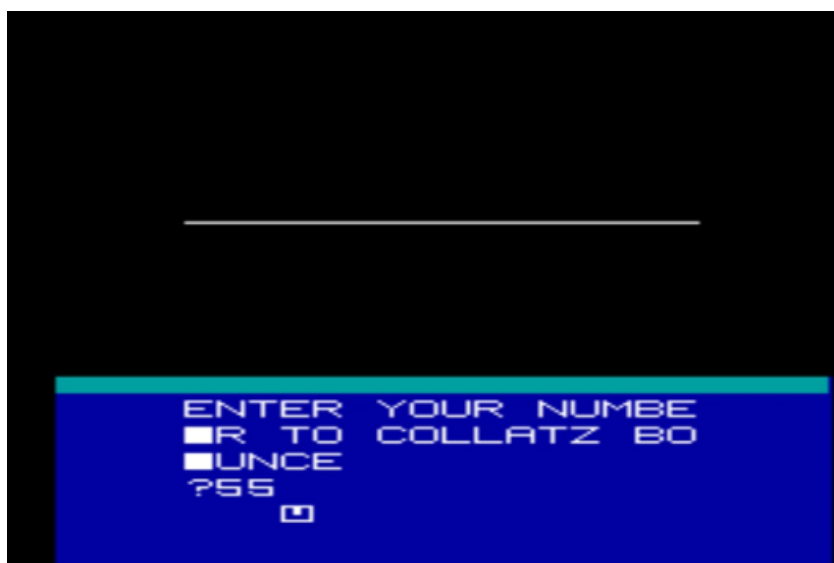
10
5
16



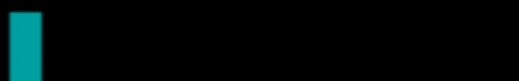
5
16
8

16
8
4





Another run, starting at 55.



■ UNCE
755
166



755
166
83



166
83
25 0



83
25 0
125



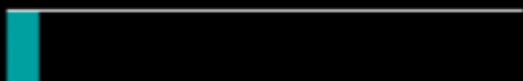
25 0
125
376



125
376
188



376
188
94



188
94
47



94
47
142



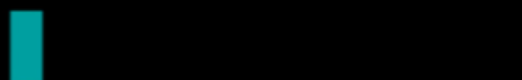
47
142
71



142
71
214



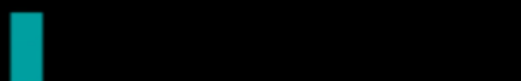
71
214
107



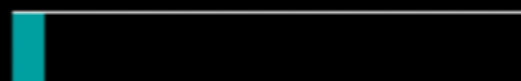
214
107
322



107
322
161



322
161
484



161
484
242

1	NUM	TOP	SCORE
55	9232	112	



A maximum value of 9232 is reached, before settling back to 1 after over a hundred bounces.

Phi and Fibonacci One-Liners

```
APL/S
(5+.5+1)×.5
1.618034
⎣
```

The value of phi, 1.618034, is easy to calculate. It can then be used to generate the Fibonacci sequence.

```
APL/S
FLOOR (.5+ < <1.61
■8♦INDEX 5) ÷ (5♦.
■5) >>
□
```

■8♦INDEX 5> ÷ (5♦.

■5>>>

1 1 2 3 5



```

FLOOR <0.5+(<(PHI=
■ <(<(Z=5♦0.5)+1)×0
■ .5)♦INDE 16)÷Z)
■

```



```

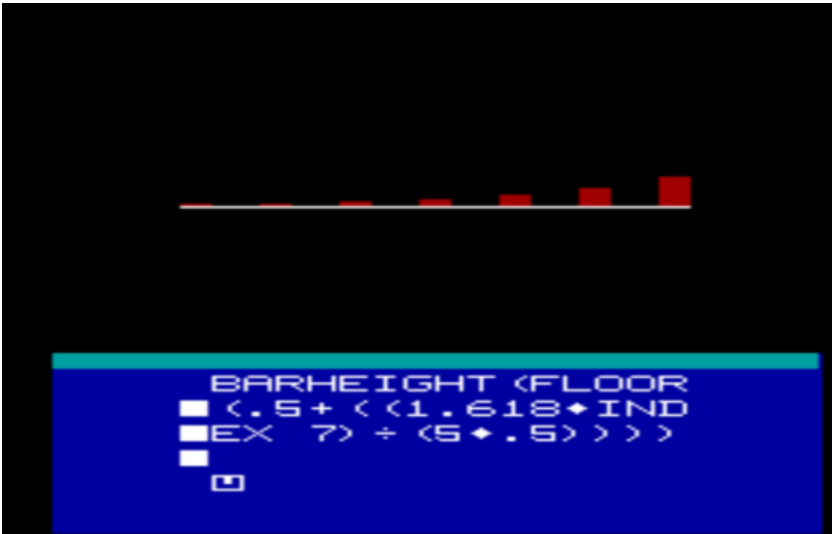
1 1 2 3 5 8 13 2
■ 1 34 55 89 144
■ 233 377 610 987

```



$\text{FLOOR} (.5 + ((\text{PHI} = ((Z = 5 * .5) + 1) \times .5) * \text{INDEX } 5) \div Z)$

The formula for the Fibonacci sequence, using Phi, as a one-liner.



Using the barchart to graph the sequence.



Add a little color. See the [APL MOOC](#) to see this done in a modern APL.

X=Y=1

PROG FIB

Z=X+Y

Z

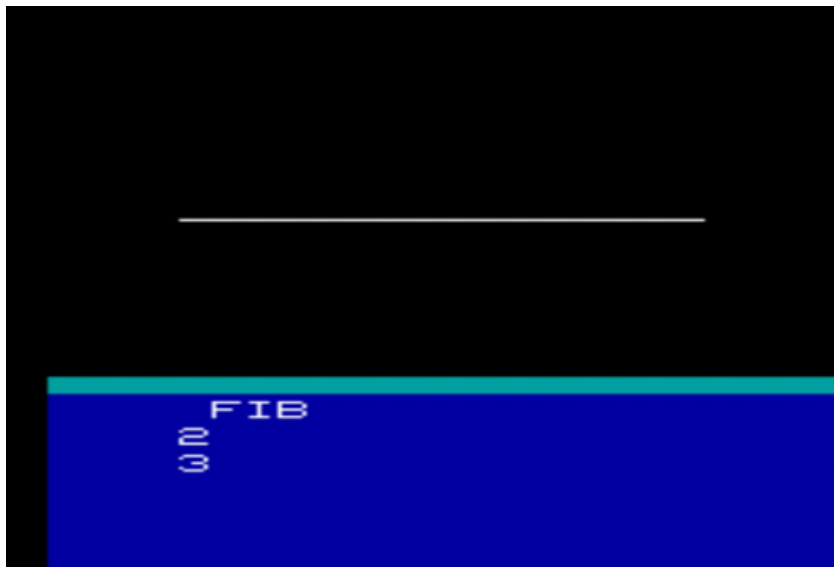
X=Y

Y=Z

FIB

ENDP

A short recursive program to list the sequence.



5
8
13

21
34
55

89
144
233

377
610
987



```
1597
2584
4181
```



```
3524578
CAPACITY 206
PROG FIB
```

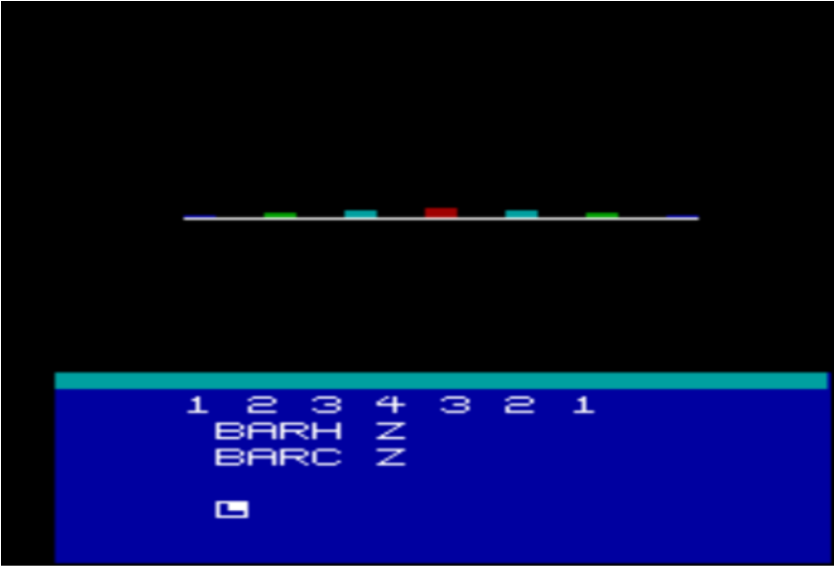
Stack overflow ends the program.

Pyramid chart

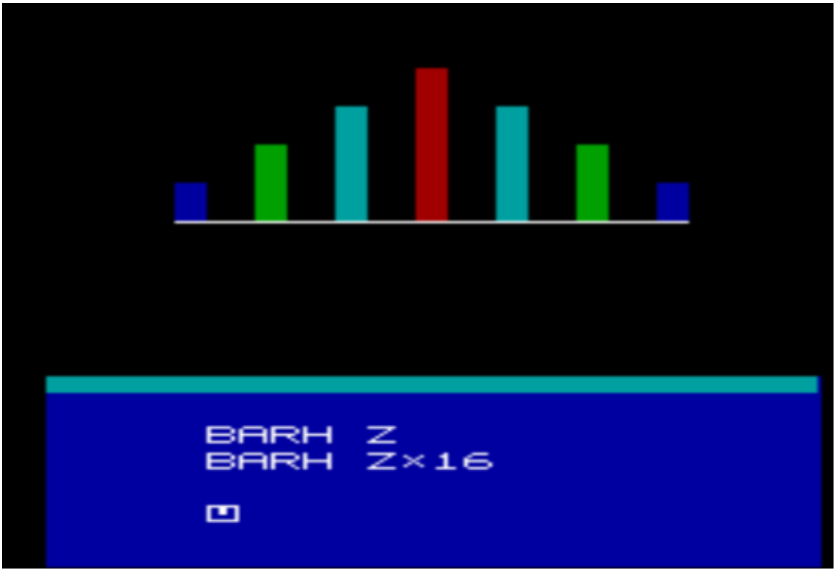
```
Z=INDE 7
Z
1 2 3 4 5 6 7
□
```

```
Z=Z MIN (8-Z)
Z
1 2 3 4 3 2 1

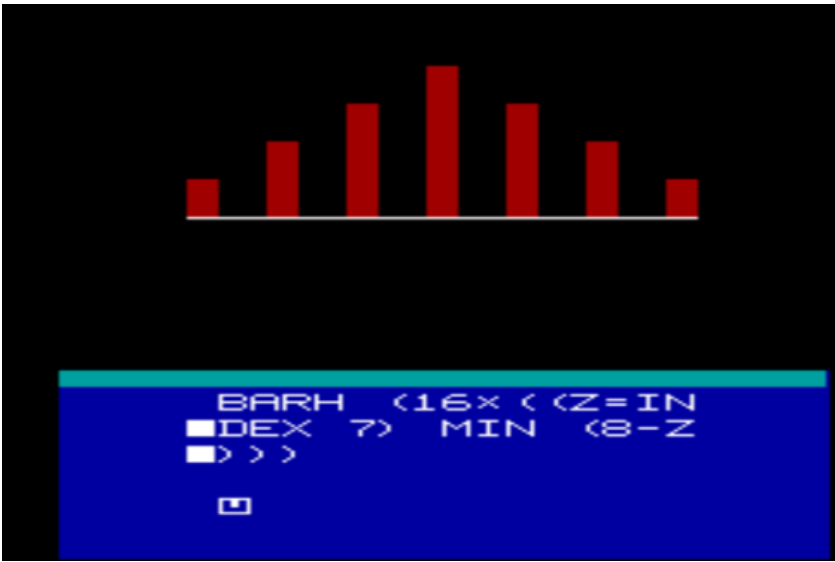
```



A small pyramid.



Scale it with multiplication.



As a one-liner.

Recursive Factorial Fun

In APL/S, recursive functions must account for all variables being global. Outside the program, set X and Y to 1, and assign the value whose factorial you want to N.

$X=Y=1$

$N=10$

PROG F

IF X LE N

THEN

$Y=Y \times X$

$X=X+1$

F

ENDI

ENDP

```
X=Y=1
Z=10
FY
□
```

```
F
Y
36288 0 0
□
```

X=Y=1

N=6

PROG F

IF X LE N

THEN

Y=Y×X

X=X+1

Y

F

ENDI

ENDP

Add a line to print the interim result, Y.

X=Y=1
Z=6
F
□

1 F
0

6
24
120

24
120
720


```
720
X=Y=1
Z=31

```

```
8.84176E30
2.652528E32
8.222838E33

```

8.222838E33

X=Y=1

N=32

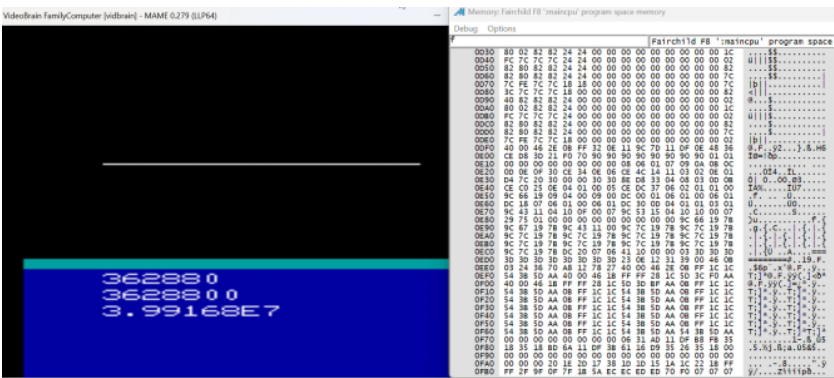
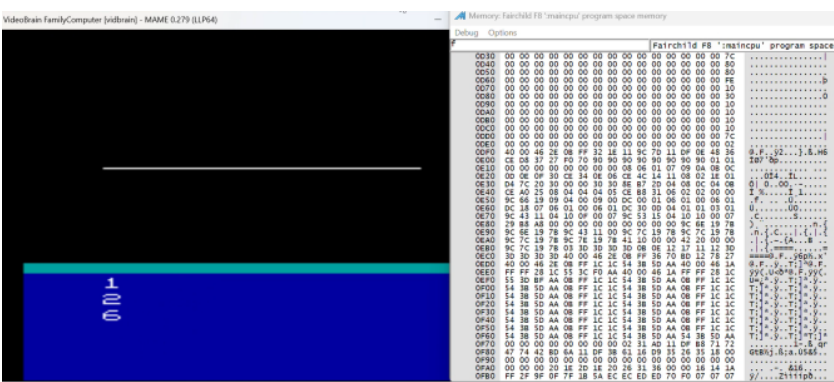
F



Capacity 206 is an “Out of stack space” error.



In the MAME debugger, you can see the stack grow as the program runs. Let's overflow the stack again while watching it fill up.



Debug Options

Fairchild f8 'maincpu' program space															
0030	00	24	02	01	82	10	02	80	02	80	00	00	00	00	FE
0040	00	34	1C	7C	7E	10	1C	F8	7C	FE	00	00	00	00	08
0050	00	24	02	80	01	10	02	80	80	82	00	00	00	00	08
0060	30	34	82	80	04	10	82	80	80	82	00	00	00	00	08
0070	30	38	7C	FE	78	7C	7C	FE	7C	FE	00	00	00	00	10
0080	00	FC	10	10	7C	7E	7C	FE	7C	FE	00	00	00	00	30
0090	00	80	80	30	30	82	80	82	80	00	00	00	00	00	10
00A0	00	80	10	10	02	80	80	00	00	00	00	00	00	00	10
00B0	00	FC	FC	10	10	7C	FE	7C	FE	00	00	00	00	00	10
00C0	00	04	04	10	10	80	80	00	00	00	00	00	00	00	10
00D0	30	84	84	10	10	80	80	84	00	00	00	00	00	00	7C
00E0	30	7C	7C	7C	7C	FE	FE	7C	FE	00	00	00	00	00	02
00F0	18	00	41	21	08	FF	FF	11	18	CF	08	11	BF	0E	40
0100	00	18	14	0A	FD	70	90	80	80	80	80	80	80	80	01
0110	00	00	00	00	00	00	00	00	08	06	01	07	09	0A	08
0120	00	0F	30	0E	34	0E	0E	0E	0E	0E	11	11	11	11	0C
0130	04	7C	20	30	00	00	30	30	FF	3A	47	09	08	08	1C
0140	CF	04	25	23	04	03	10	00	00	00	00	06	01	01	01
0150	9C	66	19	09	04	00	09	00	0C	00	01	06	01	00	06
0160	0C	1E	07	06	01	00	06	01	0C	30	00	04	01	01	01
0170	9C	43	11	04	10	0F	00	07	9C	11	04	10	04	00	07
0180	19	75	67	00	00	00	00	00	00	00	00	00	00	00	00
0190	9C	74	19	78	9C	43	11	00	9C	7C	19	78	9C	7C	19
01A0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01B0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01C0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01D0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01E0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01F0	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30
0200	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30
0210	08	0E	0E	11	11	0E	0E	17	40	40	2C	0E	FF	36	70
0220	80	11	78	27	40	1E	00	14	80	10	00	1C	1C	38	1C
0230	08	FF	1C	1C	54	38	50	AA	54	38	50	AA	58	FF	1C
0240	34	38	50	AA	08	FF	1C	1C	54	38	50	AA	54	38	50
0250	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
0260	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
0270	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
0280	7F	74	42	73	FF	35	18	7F	3F	11	35	18	35	18	00
0290	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
02A0	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
02B0	FF	2F	9F	0F	7F	18	5A	EC	EC	ED	ED	70	F0	07	07

1.55112E25

4.032913E26

1.088887E28

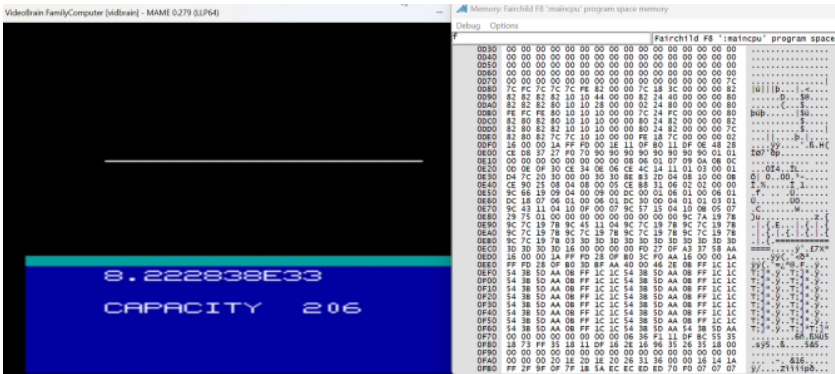
Debug Options

Fairchild f8 'maincpu' program space															
0030	00	80	80	80	80	80	80	80	80	80	00	00	00	00	7C
0040	00	FC	7C	7C	7C	7C	7C	7C	7C	FE	00	00	00	00	80
0050	00	82	84	80	04	80	82	80	80	82	00	00	00	00	80
0060	30	82	84	80	84	80	82	80	80	82	00	00	00	00	80
0070	30	7C	7C	FE	7C	FE	7C	FE	7C	FE	00	00	00	00	7C
0080	00	7C	28	10	7E	1C	FE	7C	18	00	00	00	00	00	82
0090	00	82	48	30	02	40	80	82	24	00	00	00	00	00	82
00A0	00	82	88	10	04	80	80	82	24	00	00	00	00	00	82
00B0	00	7C	FE	10	08	FC	FE	34	24	00	00	00	00	00	82
00C0	00	82	08	10	10	82	80	82	24	00	00	00	00	00	82
00D0	30	82	08	10	10	82	80	82	24	00	00	00	00	00	7C
00E0	30	7C	08	7C	10	7C	FE	18	00	00	00	00	00	00	02
00F0	40	00	46	1C	00	FF	FC	0C	11	1C	55	11	BF	0E	48
0100	00	08	1C	62	FD	70	90	80	80	80	80	80	80	80	01
0110	00	00	00	00	00	00	00	08	06	01	07	09	0A	08	0C
0120	00	0F	30	0E	34	0E	0E	0E	0E	14	11	48	02	0C	01
0130	04	7C	20	30	00	00	30	30	FF	3A	47	09	08	08	1C
0140	CF	04	25	23	04	03	10	00	00	00	00	06	01	01	01
0150	9C	66	19	09	04	00	09	00	0C	00	01	06	01	00	06
0160	0C	1E	07	06	01	00	06	01	0C	30	00	04	01	01	01
0170	9C	43	11	04	10	0F	00	07	9C	11	04	10	04	00	07
0180	19	75	67	00	00	00	00	00	00	00	00	00	00	00	00
0190	9C	7C	19	78	9C	43	11	00	9C	7C	19	78	9C	7C	19
01A0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01B0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01C0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01D0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01E0	9C	7C	19	78	9C	7C	19	78	9C	7C	19	78	9C	7C	19
01F0	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30
0200	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30
0210	08	0E	0E	11	11	0E	0E	17	40	40	2C	0E	FF	36	70
0220	80	11	78	27	40	1E	00	14	80	10	00	1C	1C	38	1C
0230	08	FF	1C	1C	54	38	50	AA	54	38	50	AA	58	FF	1C
0240	34	38	50	AA	00	46	FF	75	1C	1C	54	38	50	AA	54
0250	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
0260	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
0270	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
0280	7F	74	42	73	FF	35	18	7F	3F	11	35	18	35	18	00
0290	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
02A0	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00
02B0	FF	2F	9F	0F	7F	18	5A	EC	EC	ED	ED	70	F0	07	07

8.84176E30

2.652528E32

8.222838E33



After reaching capacity, the stack overflows.



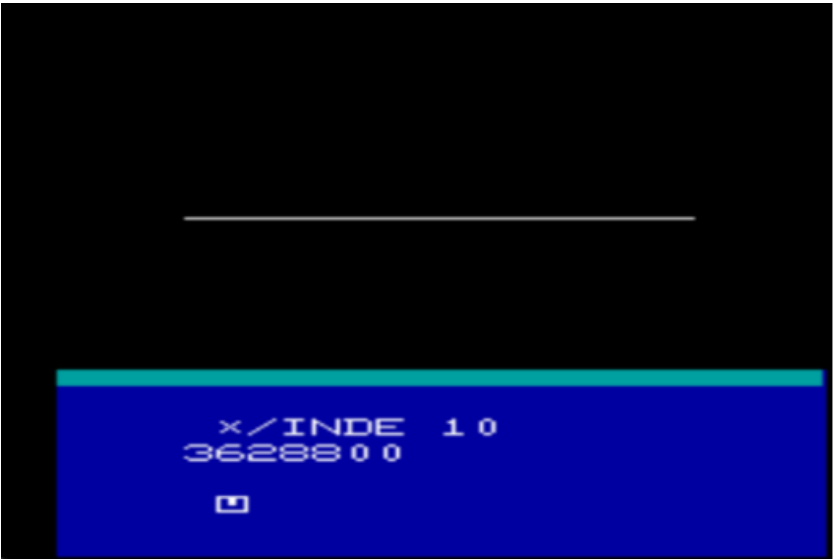
In APL/S, factorial uses the ! symbol.

■ 55
1.26964E73

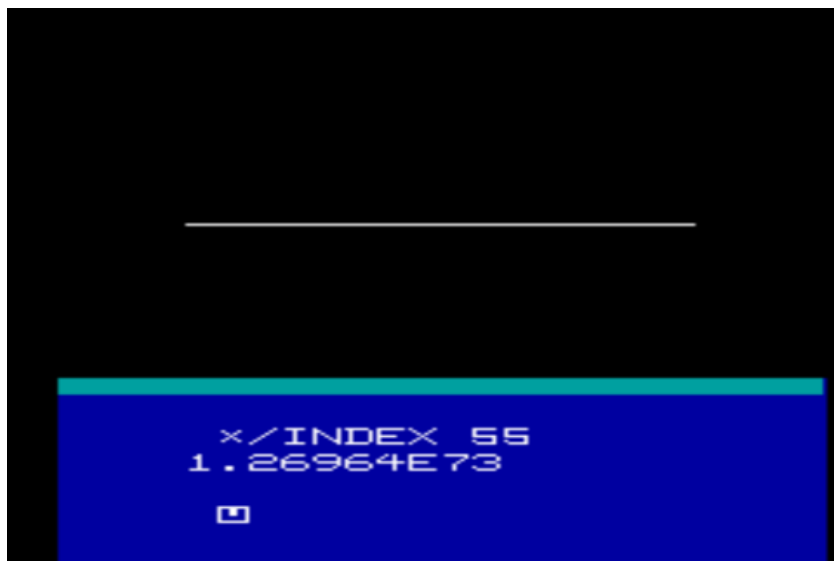




Barheight accepts values over 64 but cuts them off.



Times reduction can also be used to compute factorials.



Lunar Lander

This program is a port of David Ahl's 1973 BASIC game [ROCKT1](#).
Be sure to check the APL/S product brochure for another [version](#) of
Lunar Lander.

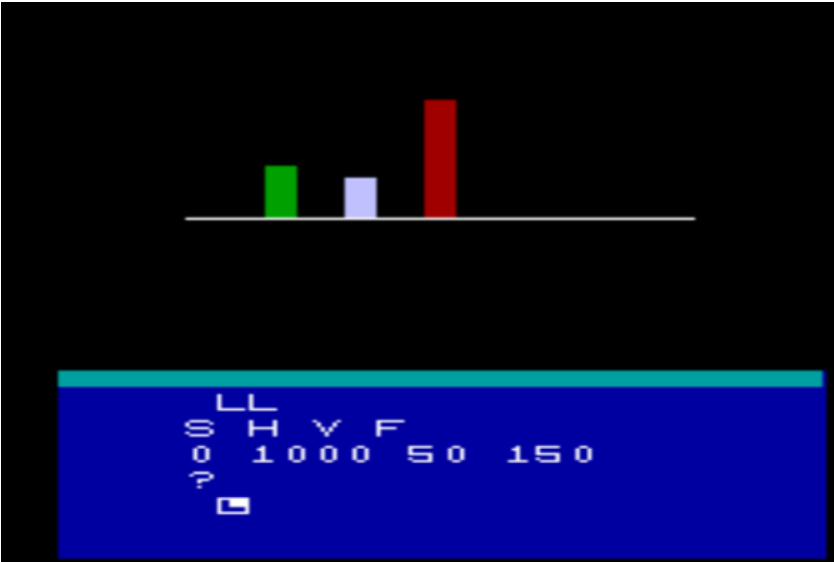
PROG LL

T=0

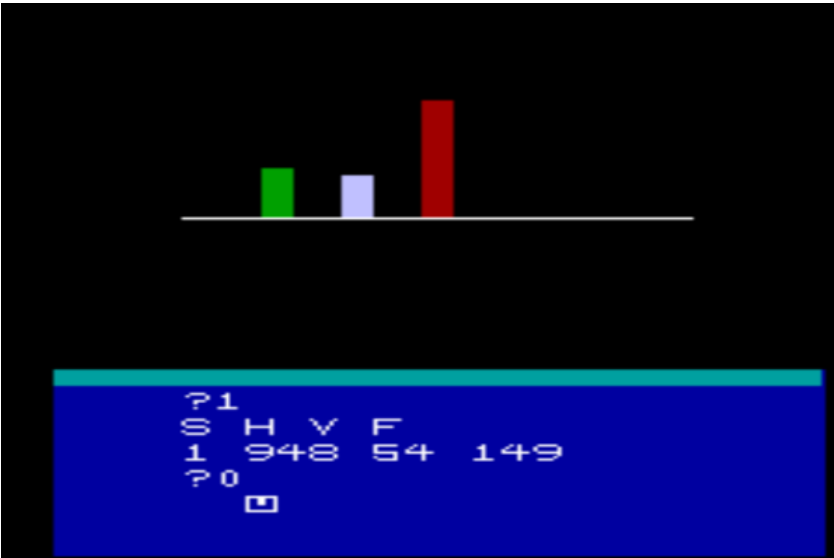
```

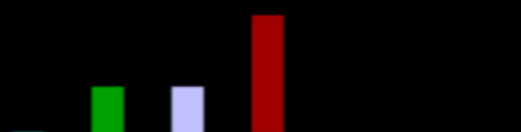
PROG LL
T=0
H=1000
V=50
F=150
BARC 3 2 9 4
WHILE H GT 0
DO
  "S H V F"
  T,H,V,F
  BARH T,(H+15),V,F+3
  B=KEYB
  IF B GT F
  THEN B=F
  ENDI
  V1=V-B+5
  F=F-B
  H=H-0.5x(V+V1)
  IF H GT 0
  THEN
    T=T+1
    V=V1
    IF F LE 0
    THEN "OUT OF FUEL"
      WHILE H GT 0
      DO
        T,H,V,F
        BARH T,(H+15),V,F+3
        V1=V+5
        H=H-0.5x(V+V1)
        T=T+1
        V=V1
      ENDW
    ENDI
  ELSE EXIT
  ENDI
ENDW
"S H V F"
T,H,V,F
"CONTACT"
ENDP

```



A sample run.





```

20
55 H V F
80 891.5 59 149
20
5

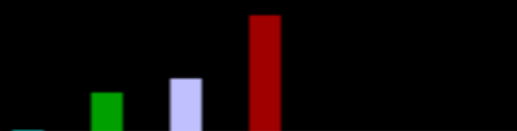
```



```

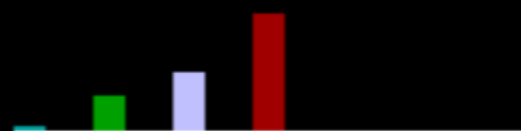
?0
$ H V F
3 830 64 149
?0

```



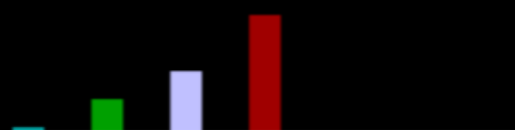
```

? 0
S H V F
4 763.5 69 149
? 0
  
```



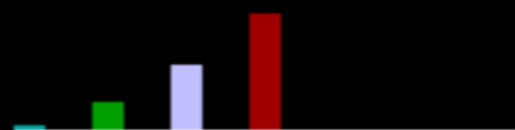
```

? 0
S H V F
5 692 74 149
? 0
  
```



```

?0
S H V F
6 615.5 79 149
?0
  
```



```

?0
S H V F
7 534 84 149
?44
  
```



```

?44
S H V F
8 469.5 45 105
?0
  
```



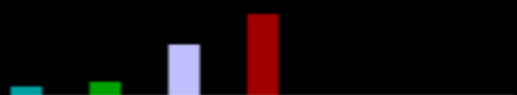
```

?0
S H V F
10 369.5 55 105
?
  
```




```

? 0
S  H  V  F
11  312  60  105
?
  
```



```

? 0
S  H  V  F
12  249.5  65  105
?
  
```



```
?22
S H V F
13 193 48 83
?
  
```



```
?0
S H V F
14 142.5 53 83
?
  
```



?0
S H V F
15 87 58 83
?
□



?33
S H V F
16 43 30 50
?
□



?5
S H V F
17 13 30 45
?
□



S H V F
17 13 30 12
CONTACT
□

Unit Circle

In his September, 1980 ACM Queue paper “[Uniform sampling on simplices and spheres](#),” mathematician Balder Von Hohenbaeken details his APL implementation of an algorithm presented by [Donald Knuth in *The Art of Computer Programming, Volume 2: Seminumerical Algorithms*](#). Knuth shows how to use the polar method for generating normalized random deviates, developed by [Box, Muller, and Marsagli](#). We will use Von Hohenbaeken’s technique to generate and display unit circles using APL/S.

```

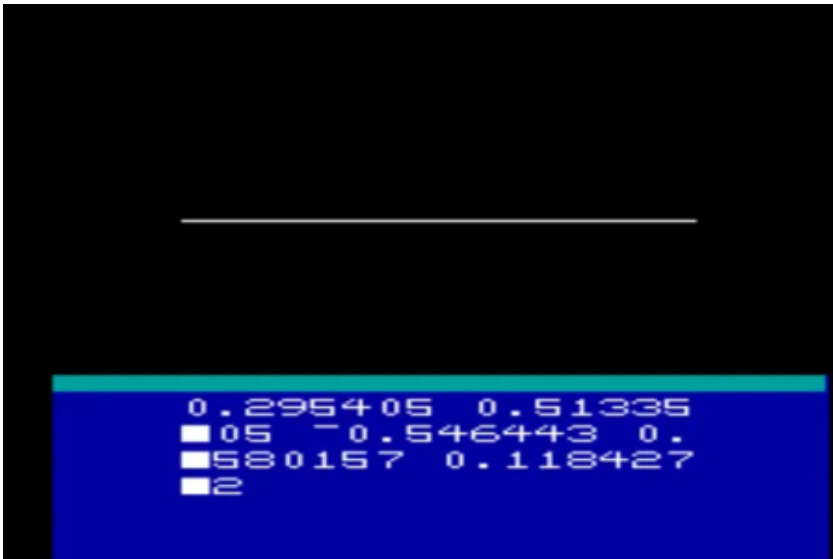
G=ARRAY 7

PROG UNI
BARC INDEX 7
X=INDEX 0
D=2
WHILE D GT SIZE X
DO
    WHILE 1
    DO
        V= -1+2*31
        V= -1+((RAND(2*V,(2*V)))+V)
        IF 1 GT (S-+/(V*2))
        THEN
            EXIT
        ENDI
    ENDW
    X=X,V*(((-2*LOG S)+S)*.5)
ENDW
IF 1 EQ (D MOD 2) // odd dimensions 3, 5, 7 etcetera
THEN
    M=ARRAY D
    MI=1
    WHILE MI LE D
    DO
        M(MI) = X(MI)
        MI=MI+1
    ENDW
    X=M
ENDI
X=X÷(+/(X*2)*.5)
X
IF D EQ 2
THEN
    I=CEIL (3.5+(X(1)×3))
    H=CEIL (X(2)×64)
    G(I) = H
    BARH G
ENDI
ENDP

```

In APL/S, all variables are globals. Before running the program, first prepare a global array to store the bar graph height values. As the program is run multiple times, the bar graph will accumulate coordinates.

The [Box-Muller-Marsagli-Knuth](#) method can generate coordinates for any dimension, although for our unit circle visualization we will only use $D=2$. This APL/S implementation can compute coordinates for spheres of higher dimension. Let's try an example run with $D=5$:



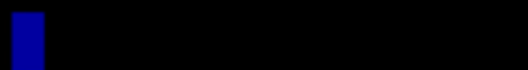
It's easy to check these coordinates using a calculator:

$$\text{sqr}(0.2954) + \text{sqr}(0.51335) + \text{sqr}(-0.5464) + \text{sqr}(0.58015) + \text{sqr}(0.1184) = \text{>}$$

0.999934925

For odd-numbered dimensions, special handling is required since the algorithm generates $X[1]$, $X[2]$ pairs. In the odd cases of $D=3$, $D=5$, $D=7$, ... the line "IF 1 EQ (D MOD 2)" evaluates as true and then, somewhat awkwardly, a new array is created and all the pairs are copied into the new array except for the last pair, where only one member of the pair comes over. This newly created array has "dropped" half a pair, leaving an odd-numbered count of random deviates, done this way because there is no Drop in APL/S. After this, the norm of the resulting vector is computed as usual with $X = X \div (+/(X*2)*.5)$.

Finally, the program checks if $D=2$, and if so, scales and shifts the unit circle coordinates to ready them for bar graphing. The VideoBrain's [bar graph facility offers 7 bars, with each bar capable of displaying values from -64 to +64](#). We can directly visualize the unit circle using this facility:



UNI
-0.924785 0.3804
■92



UNI
-0.2218381 0.975
■083

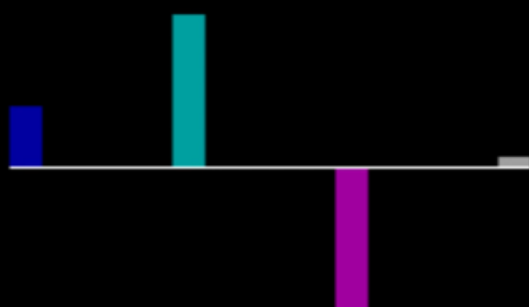
UNI





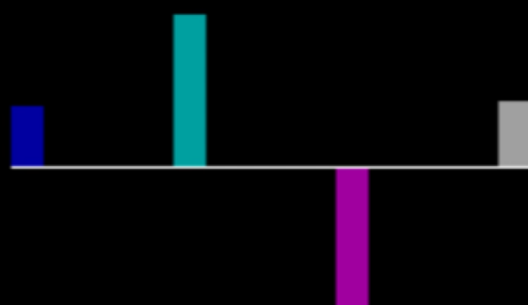
```

UNI
0.998452  0.05561
■ 04
UNI
  
```

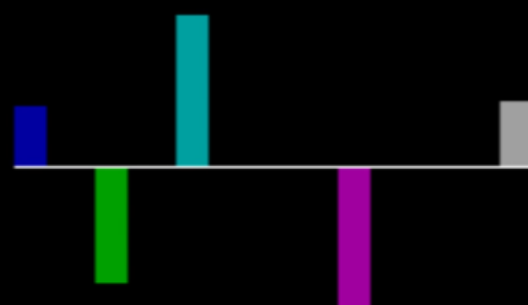


```

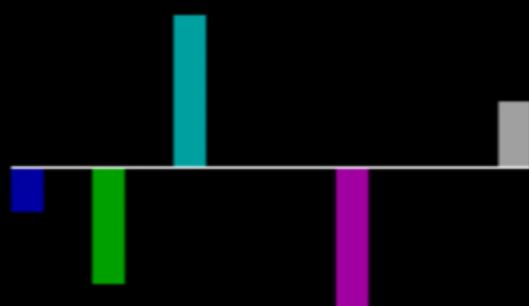
UNI
0.37533  -0.92689
■ 2
UNI
  
```



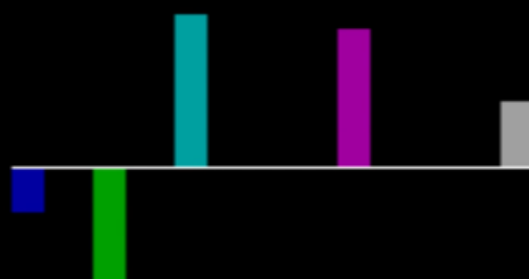
UNI
0.908808 0.41721
■53
UNI
□



UNI
-0.647676 -0.761
■916
UNI
□

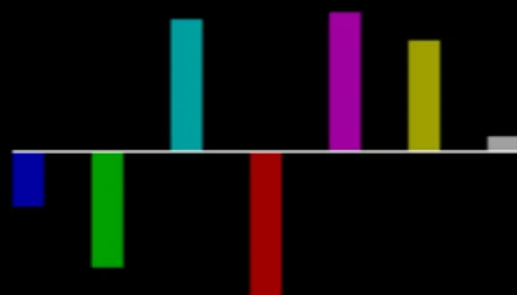


UNI
 -0.958435 -0.285
 ■3103



UNI
 0.4839674 0.875 0
 ■86

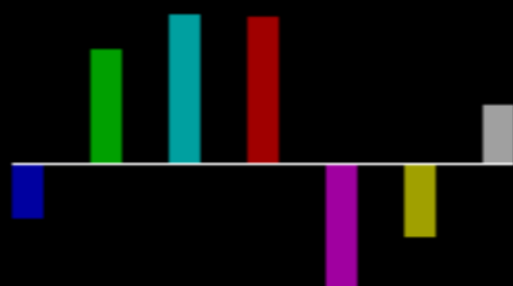




U
-0.4972747 0.867
■594
□

Another example of showing points being added to a unit circle chart.





■ 141
- 0.870031 - 0.492
■ 9972



For more, including Commodore 64, C128, and SuperPET implementations, see “[Using APL to Visualize the Unit Circle on Vintage 8-bit Computers](#)”

Dicejack

A dice version of Blackjack, similar to the game “[Twenty-One](#)” from “The Gateway Guide To The ZX81 And ZX80” by [Mark Charlton](#). The book is part of the Creative Computing material released into the public domain by David Ahl.

```

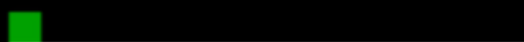
PROG D
BARC 2 3
BARH +/(Z=Rand 6 6),0
Z
WHIL 1
DO
    'HIT? 1/0'
    C=KEYB
    IF C EQ 0
    THEN EXIT
    ENDI
    IF C EQ 1
    THEN Z=Z,RAND 6
        Z
        BARH +/Z
        IF +/Z GT 21
        THEN "BUSTED"
            EXIT
        ENDI
    ENDI
ENDW
+/Z
IF +/Z LE 21
THEN
    B=0 //DEALER NOT BUSTED
    X=Rand 6 6
    X
    WHIL (+/Z) GE (+/X)
    DO
        X=X,RAND 6
        X
        BARH +/Z,+/X
        IF +/X GT 21
        THEN "I BUSTED"
            B=1
            EXIT
        ENDI
    ENDW
    +/X
    IF B EQ 1
    THEN "YOU WIN"
    ELSE
        IF +/X GT +/Z
        THEN "I WIN"
        ELSE "YOU WIN"
        ENDI
    ENDI
ENDI
ENDP

```

D
3 3
HIT? 1/0
?1
E



?1
3 3 3
HIT? 1/0
?1
□



?1
3 3 3 4
HIT? 1/0
?1
□



?1
3 3 3 4 5
HIT? 1/0
?0
□



18
4 20
4 20 20



4	2	2	1		
4	2	2	1	2	
4	2	2	1	2	3



4 2 2 1 2 3 5

19

I WIN





DJ
4 1
HIT? 1/0
?1
□

Another game.





P1
4 1 1 4
HIT? 1/0
P1
□



?1
4 1 1 4 3
HIT? 1/0
?1
□



?1
4 1 1 4 3 5
HIT? 1/0
?0
□



70
18
3 3



3	3	3		
3	3	3	4	
3	3	3	4	5



3 3 3 4 5 6
I BUSTED
24



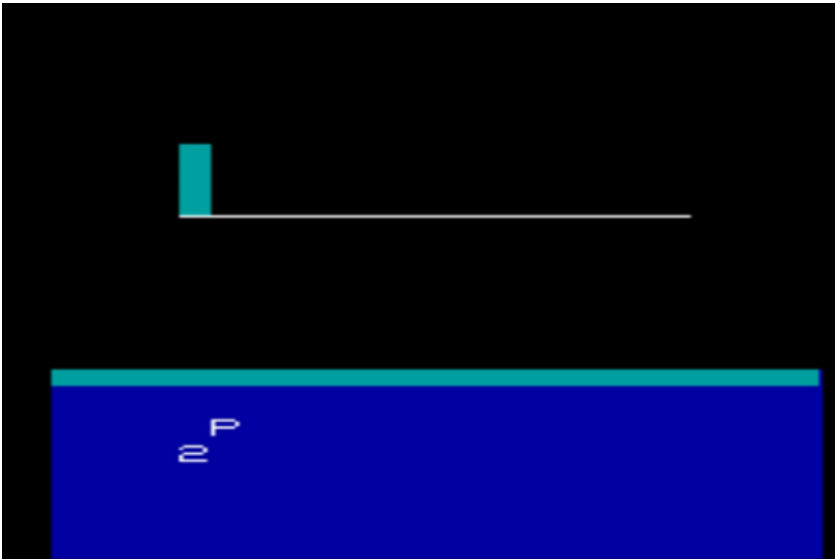
I BUSTED
24
YOU WIN



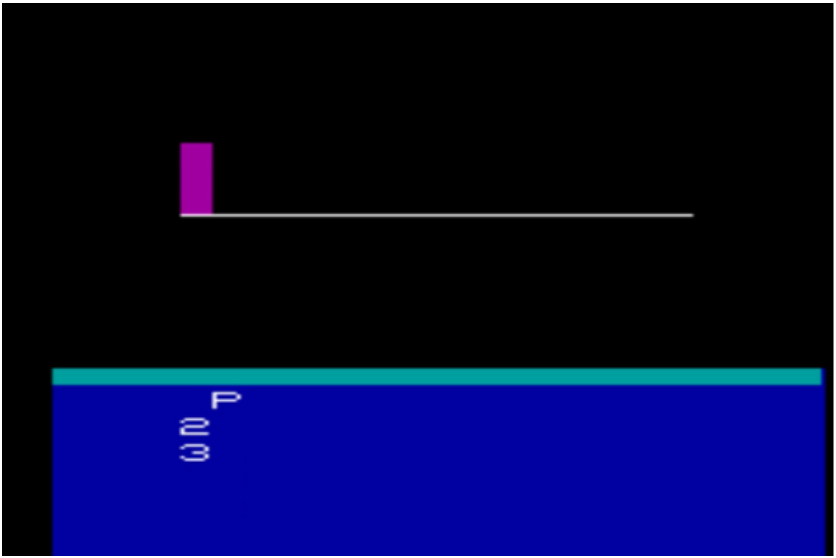
Primes

```
PROG P
BARC 2
BARH 30
2
BARC 3
3
I=4
UPTO=23
WHIL I LE UPTO
DO
  PRIM=1
  IF I MOD 2 EQ 0
  THEN PRIM=0
  ELSE
    J=3
    WHIL J LE (I * .5)
    DO
      IF I MOD J EQ 0
      THEN PRIM=0
      EXIT
      ELSE J=J+2
    ENDI
  ENDW
  ENDI
  BARC 1+(I MOD 7)
  IF PRIM EQ 1
  THEN BARH 30
  I
  ELSE
    BARH -30
  ENDI
  I=I+1
ENDW
ENDP
```

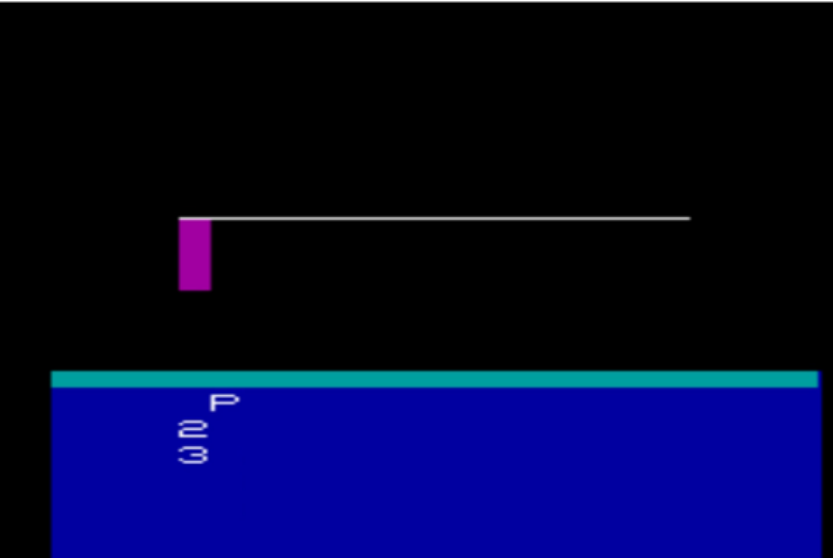
First, consider a program that uses a [primality by trial division algorithm](#).



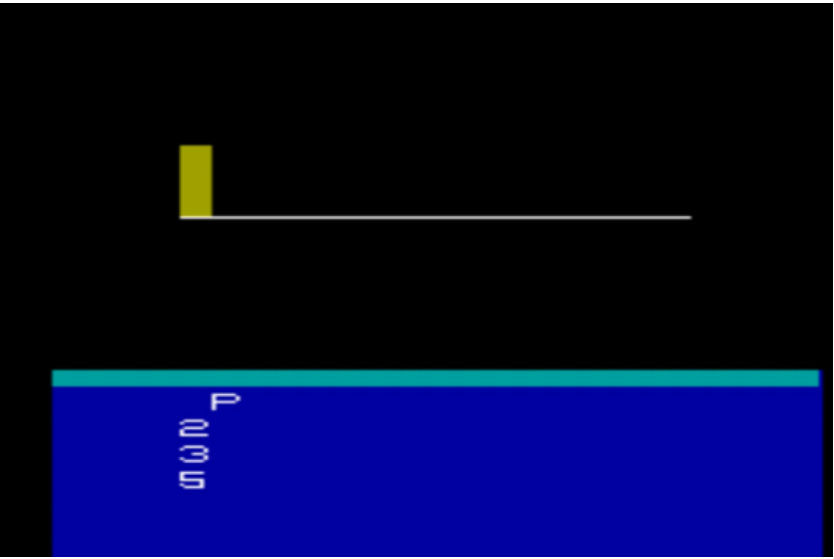
2 is prime, so the flag goes up to indicate a prime was found.



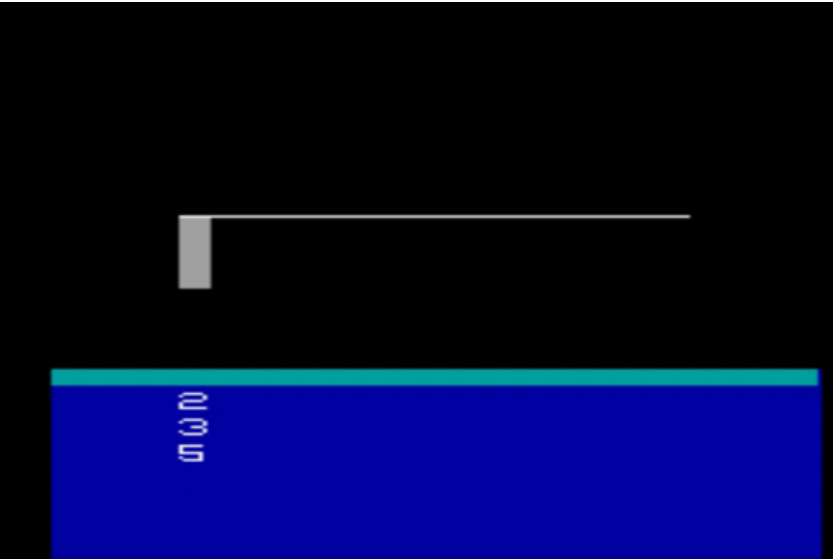
3 is also prime, the flag remains up and shifts color accordingly.



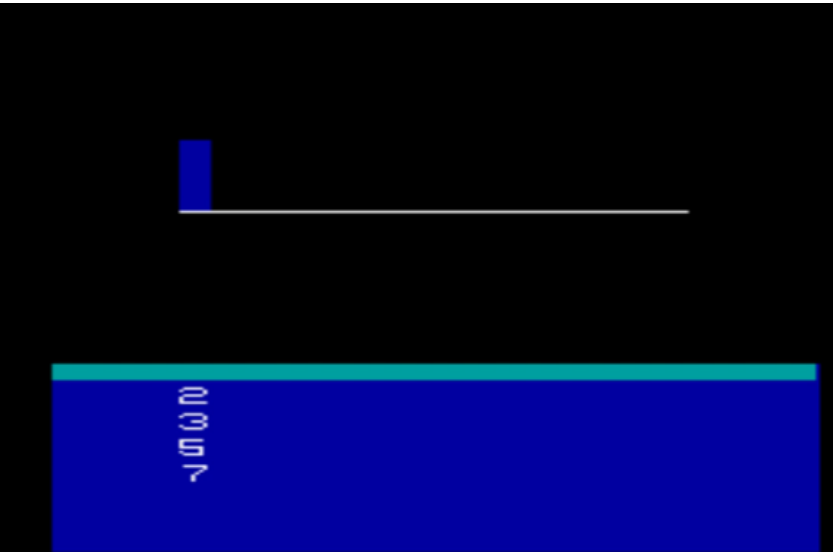
Down for 4.



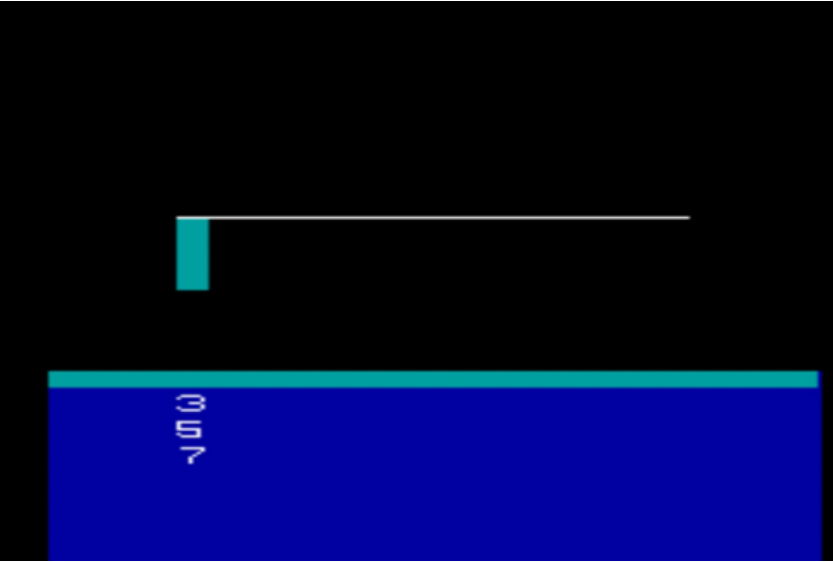
Up for 5.



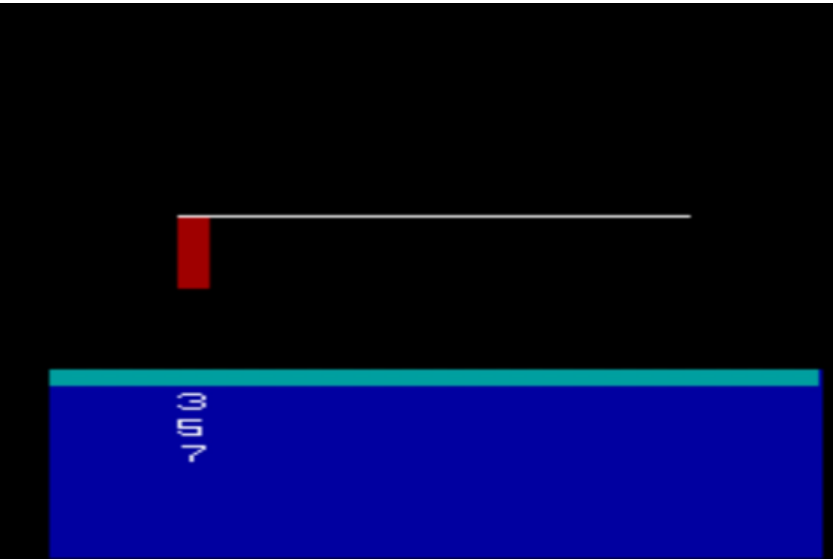
Down for 6.



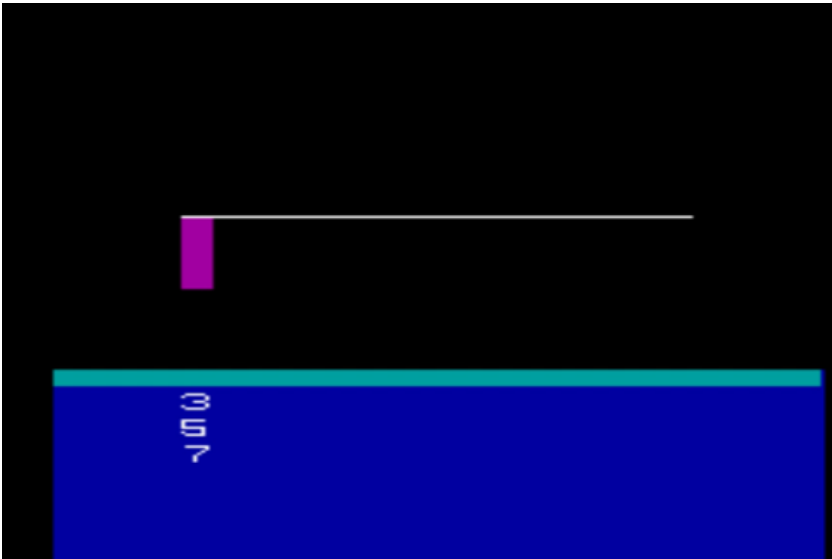
Up for 7.



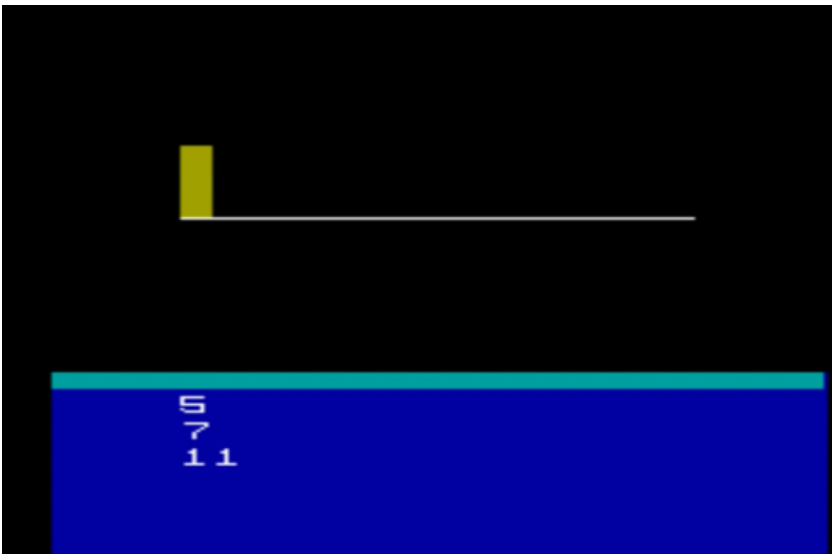
Down for 8.



Down for 9.



Down for 10.



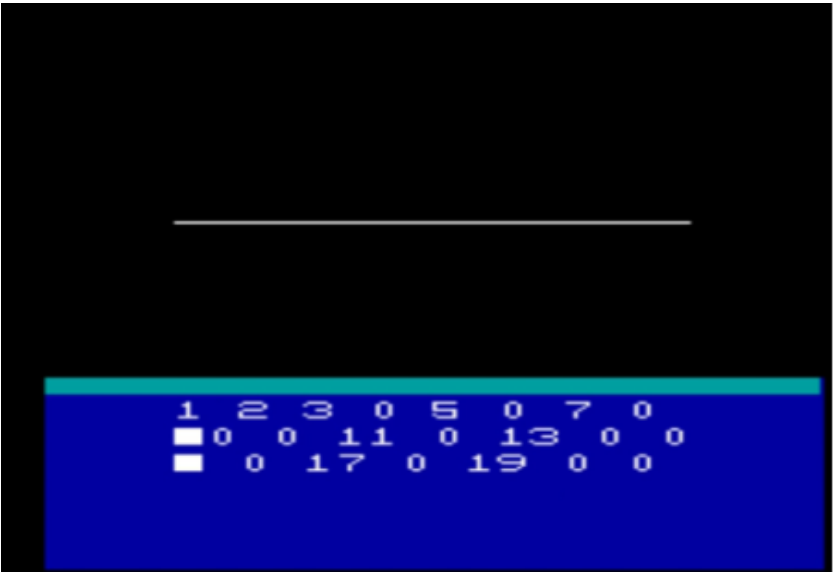
Up for 11. This method is fairly slow. The algorithm requires an increasing amount of time as the numbers being checked grow larger.

Next, consider a different algorithm for finding primes, the [Sieve of Eratosthenes](#).

```
PROG SIEVE
N=INDEX 198
I=2
WHIL I LE SIZE N * .5
DO
    IF N(I) EQ 0
    THEN EXIT
    ELSE
        J=I x I
        WHILE J LE SIZE N
        DO
            N(J)=0
            J=J+I
        ENDW
    ENDI
    I=I+1
ENDW
N
ENDP
```

SIZE N
198
S

To run the sieve for numbers up to and including 198, start by creating an array using index 198.



Run the program and the array will be listed, with every number but the primes zeroed out.

■	0	23	0	25	0	0	0
■	29	0	31	0	0	0	
■	35	0	37	0	0	0	4

Only the primes remain when the array is printed.



However, we are constrained by memory, and can only compute primes up to the size of the largest array the system can store.

17
19
23

0 0 0 89 0 91 0
0 0 95 0 97 0
0 0



Comparing the speed of the two algorithms (with the bar chart primality indicators removed), the sieve method can list all primes under 100 before the slower algorithm can list a prime above 23.

37
41
43

■ 0 185 0 187 0
■ 0 0 191 0 193 0
■ 0 0 197 0



It can print all primes up to 198 before the slower method can compute a prime above 43.

Data Statistics

A program to calculate statistics about a data set. For a given set of numbers, the program will list the minimum, maximum, range and sum of the data, the size of the data set, the mean, variance, [standard deviation](#), sample variance, and [sample standard deviation](#).

```
PROG DSTATS
"ENTER YOUR DATA"
X=KEYB
"DATA ENTERED"
X
"MINIMUM"
MIN/X
"MAXIMUM"
MAX/X
"RANGE"
MAX/X - MIN/X
"SUM"
+/X
"SIZE OF DATA SET"
N=SIZE X
N
"MEAN"
M=(+/X)÷N
M
"VARIANCE"
V=+/((X-M)*2)÷N
V
"STD DEV"
V*.5
"SAMPLE VARIANCE"
V=+/((X-M)*2)÷(N-1)
V
"SAMPLE STD DEV"
V*.5
ENDP
```

ENTER YOUR DATA
798 97.5 81.5 76
■ 69

A sample run.

DATA ENTERED
98 97.5 81.5 76
■69
MINIMUM
69
MAXIMUM
98
RANGE
29
SUM
42
SIZE OF DATASET
5
MEAN
84.4
VARIANCE
134.54
STD DEV
11.59914
SAMPLE VARIANCE
168.175
SAMPLE STD DEV
12.96823



Lotto Picker

Choose five non-repeating numbers between 1 and 69, and an additional bonus number between 1 and 26. In this algorithm we explicitly model each of the 69 main balls in an array and zero them out as they are selected, checking each time if the selected ball is already zeroed or not.

```
PROG LOTTO

// Pick 5 between 1 and 69
// Pick 1 between 1 and 26

B=INDEX 69
P=RAND 26
W=ARRAY 5
C=1
WHILE C LE 5
DO
    R=RAND 69
    IF B(R) NE 0
    THEN
        W(C)=R
        B(R)=0
        C=C+1
    ENDI
ENDW
W,P
BARC INDEX 6
BARH .9x(W,P)
ENDP
```



R
L
22 52 27 65 26 5
□

Sample run.

PROG LOTTO2

// Pick 5 BETWEEN 1 and 69

// Pick 1 between 1 and 26

P=RAND 26

W=ARRAY 5

C=1

WHILE C LE 5

DO

 R=RAND 69

 IF (+/ (R EQ W) EQ 0)

 THEN

 W(C)=R

 C=C+1

 ENDI

ENDW

W,P

BARC INDEX 6

BARH .9x(W,P)

ENDP

A different method uses add reduction instead, requiring less much storage.

Estimate Pi

This program uses a Monte Carlo algorithm to estimate the value of pi.

```
PROG PI
IN=0
C=1
"HOW MANY ITERATIONS?"
I=KEYB
WHILE C LE I
DO
    X=(RAND 1000000) ÷ 1000000
    Y=(RAND 1000000) ÷ 1000000
    D=(X×X)+(Y×Y)
    IF D LE 1
    THEN IN=IN+1
    ENDI
    C=C+1
ENDW
(4×IN) ÷ I
ENDP
```

```
PI
HOW MANY ITERATI
■ONS?
?100
  
```

```
■ONS?
?100
2.96
  
```

PI
HOW MANY ITERATI
■ONS?
?5 0 0
□

■ONS?
?5 0 0
3. 088
□

```

PROG PI
IN=0
C=1
"HOW MANY ITERATIONS?"
I=KEYB
WHILE C LE I
DO
    X=(RAND 1000000) ÷ 1000000
    Y=(RAND 1000000) ÷ 1000000
    X,Y
    D=(X×X)+(Y×Y)
    IF D LE 1
    THEN IN=IN+1
        BARC C
        BARH 30
    ELSE
        BARC C
        BARH -30
    ENDI
    C=C+1
ENDW
(4×IN) ÷ I
ENDP

```

We can use the bar chart to show if the random points fall in the unit circle, to visualize the process.

The bar chart value will be positive or negative depending on if the point is in the unit circle.

PI
HOW MANY ITERATI
■ONS?
?100
■



?100
0.364815 0.75293
■9



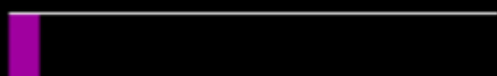
0.364815 0.75293
■9
0.86962 0.550829



■9
0.86962 0.550829
0.808958 0.75081



0.808958 0.75081
0.441977 0.97916
■ 1



0.441977 0.97916
■ 1
0.76218 0.864406



0.76218 0.864406
0.323971 0.66121
■1



■1
0.154152 0.38503
■3



After 100 points are checked, the estimated value of pi is 3.12.

Taylor, Maclaurin, and Madhava-Leibniz Series

See <https://www.mathsisfun.com/algebra/taylor-series.html>

Exponential

$$e^x = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$$

Sine

$$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$$

Cosine

$$\cos(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$$

Arctan (Leibniz Pi)

$$\arctan(1) = \frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots$$

```

PROG TAYLOR
X=5
TICK=1
N=22
I=1
E=1
S=0
C=1
A=0
WHIL I LE N
DO
    E=E+(X*I÷!I)
    IF I MOD 2 EQ 0
    THEN
        TICK=-1×TICK
        C=C+(TICK×(X*I÷!I))
    ELSE
        S=S+TICK×(X*I÷!I)
        A=A+TICK×(1÷I)
    ENDI
    I=I+1
ENDW
E,S,C,(A×4)
ENDP

```

T
148.4136 -0.9589
■15 0.2836481 3.
■232315

Running the program for $X=5$, extending out to 22 terms. Arctan is multiplied by 4 to get an approximation of pi.

Stag Hunt

In game theory, the stag hunt models a tension between individual safety and mutual cooperation.

Two hunters independently choose between pursuing a large prey that requires cooperation or settling for a smaller one they can obtain alone. Hunting the larger animal succeeds only if both participants commit. If either defects, the attempt fails. By contrast, the smaller prey can always be caught individually, but yields a much lower payoff. Each participant faces a tradeoff between the certainty of a modest reward and the risk of aiming for a larger shared benefit.

```

PROG STAG
WHIL 1
DO
    BARH 0 0 0
    'STAG OR HARE? 1 OR 0"
    I=KEYB
    IF I EQ 99
    THEN EXIT
    ENDI
    C=-1+RAND 2
    IF I EQ 1
    THEN
        IF C EQ 1
        THEN
            "I CHOSE STAG TOO"
            Q=10
        ELSE
            "I CHOSE HARE."
            Q=1
        ENDI
    ELSE
        IF C EQ 0
        THEN
            "I CHOSE HARE TOO"
            Q=5
        ELSE
            "I CHOSE STAG."
            Q=1
        ENDI
    ENDI
    BARC 2 3 4
    BARH ((-20+I*40),(-20+C*40),(Q*6))
    'YOUR PAYOUT IS"
    Q
ENDW
ENDP

```

S
STAG OR HARE? 1
■OR 0
?1
□

A sample run.





STAG OR HARE? 1
■OR 0
?1



?1
I CHOSE HARE.
YOUR PAYOUT IS
1



STAG OR HARE? 1
■OR 0
? 0
I CHOSE HARE TOO



? 0
I CHOSE HARE TOO
YOUR PAYOUT IS
5



STAG OR HARE? 1
■ OR 0
? 0



? 0
I CHOSE STAG.
YOUR PAYOUT IS
1

Moo

Moo, or Bulls and Cows, is a classic code-guessing game. The computer chooses a hidden number and the player attempts to discover it through successive guesses, using feedback from each attempt to narrow the possibilities. The game relies entirely on logical deduction rather than chance. As written, the program reveals the code for demonstration purposes, so remove the line where the code is printed to play the game.

The computer selects a three or four digit number with no repeated digits. After the player guesses, the computer reports how many digits are correct and correctly placed (red “bulls”) and how many are correct but in the wrong position (white “cows”).

Long before modern commercial adaptations such as *Mastermind*, the game circulated informally and appeared early in computing culture. During the 1970s it was implemented on time-shared mainframe systems, where it was commonly known as MOO. Variants were ported to Multics and early Unix systems, and versions were distributed through user groups and software libraries for DEC machines. Implementations appeared in several languages, including BASIC and FOCAL, and a PDP-8 version later influenced a commercial version of the game released by Milton Bradley.

```

PROG MOO
WHIL 1
DO
  Z= RAND 5 5 5
  IF +/(Z(1) EQ Z) EQ 1
  THEN
    IF +/(Z(2) EQ Z) EQ 1
    THEN
      EXIT
    ENDI
  ENDI
ENDW
"GUESS THE 3 NUMBERS"
WHIL 1
DO
  I=KEYB
  IF I(1) EQ 99
  THEN
    EXIT
  ENDI
  X=+/(Z EQ I)
  IF 3 EQ X
  THEN "YOU WIN"
  EXIT
ELSE
  C=X
  J=1
  R=0
  WHIL J LE 3    //CORRECT COLOR WRONG SPOT
  DO
    IF Z(J) NE I(J)
    THEN
      R=R+ (+/(Z(J) EQ I ) )
    ENDI
    J=J+1
  ENDW
  "WHITE/RED"
  C,R
ENDI
ENDW
ENDP

```


M
5 4 2
GUESS
2 4 3

U

P1 4 3
WHILE/R=0
1 0
P4 5 1

u

P24 5 1

WE=0/R=0

0 2

P25 6 4

u

25 6 4

WHITE/RED

1 1

25 2 4

u

25 2 4
WENTZ/REID
1 2
25 4 2

u

1 2
25 4 2
YOU WIN

U

```

PROG MOO4
WHIL 1
DO
  Z= RAND 5 5 5 5
  IF +/(Z(1) EQ Z) EQ 1
  THEN
    IF +/(Z(2) EQ Z) EQ 1
    THEN
      IF +/(Z(3) EQ Z) EQ 1
      THEN
        EXIT
      ENDI
    ENDI
  ENDI
ENDW
"GUESS THE 4 NUMBERS"
WHIL 1
DO
  I=KEYB
  IF I(1) EQ 99
  THEN
    EXIT
  ENDI
  X=+/(Z EQ I)
  IF 4 EQ X
  THEN "YOU WIN"
  EXIT
  ELSE
    C=X
    J=1
    R=0
    WHIL J LE 4    //CORRECT COLOR WRONG SPOT
    DO
      IF Z(J) NE I(J)
      THEN
        R=R+(+/(Z(J) EQ I ))
      ENDI
      J=J+1
    ENDW
    "WHITE/RED"
    C,R
  ENDI
ENDW
ENDP

```

M
S 1 2 3
GUESS
P4 9 7 8

2

P4 5 7 8
WHILE/R=0
0 0
P1 2 3 4
u

P1 2 3 4

WHITE/RED

0 3

P

6

P4 3 2 1

WHERE

1 2

P

2

25 3 1 2

WHITE/RED

1 3

2

6

25 2 1 3
3 4 7 2
0 0
2

5

22

25 1 2 3

YOU WIN

5

Ecte's Guess

A port of David Ahl's [GUESS](#). Dedicated to my friend Ecte, who enjoys porting this game to new languages.

```

PROG GUES
BARC 3
  "WHAT LIMIT DO YOU WANT"
  LIM=KEYB
  COUNT=1
  NUM=RAND LIM
  "OK I CHOSE A NUMBER. WHAT IS YOUR GUESS"
  WHILE NUM NE G=KEYB
  DO COUNT=COUNT+1
    IF G LT NUM
    THEN "TOO LOW"
      BARH -30
    ELSE "TOO HIGH"
      BARH 30
    ENDIF
    "GUESS AGAIN"
  ENDWHILE
  BARH 0
  "YOUR SCORE VERSUS BINARY SEARCH"
  COUNT, (1+ FLOOR (LOG LIM ÷ LOG 2))
ENDP

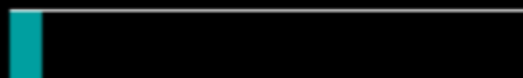
```

GUES
WHAT LIMIT DO YO
■U WANT?
?100
□

OK I WILL CHOSE
■ A NUMBER. WHAT
■ IS YOUR GUESS
?
■



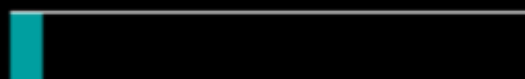
?26
TOO HIGH
GUESS AGAIN
?12
□



?12
TOO LOW
GUESS AGAIN
?19
□



?19
TOO HIGH
GUESS AGAIN
?15
□



?15
TOO LOW
GUESS AGAIN
?17





?17
TOO HIGH
GUESS AGAIN
?16
□

?16
YOUR SCORE VERSU
■S BINARY SEARCH
6 7

Recursive Coin Change Maker

This program counts out coins to give as change.

Outside the program, set $Q = D = N = P = 0$, and set X to the amount of money to count.

$$Q = D = N = P = 0$$

Q=D=N=P=0

X=89

PROG C

IF X GE 25

THEN Q=Q+1

 X=X-25

ELSE

 IF X GE 10

 THEN D=D+1

 X=X-10

 ELSE

 IF X GE 5

 THEN N=N+1

 X=X-5

 ELSE

 P=X

 X=0

 ENDI

 ENDI

ENDI

"X Q D N P"

X,Q,D,N,P

IF X GT 0

 THEN C

ENDI

ENDP

```
X=89
Q=D=N=P=0
C
□
```

```
      C
X  Q  D  N  P
64 1  0  0  0
```

64	1	0	0	0
X	Q	D	N	P
39	2	0	0	0

14	3	0	0	0
X	Q	D	Z	P
4	3	1	0	0

4	3	1	0	0
X	Q	D	Z	P
0	3	1	0	4



```
X=41
CQ=D=N=P=0
□
```

	C				
X	Q	D	N	P	
16	1	0	0	0	

S	1	1	0	0
X	Q	D	Z	P
1	1	1	1	0

1	1	1	1	0
X	Q	D	Z	P
0	1	1	1	1



Calendar Clock

Enter in the program, but before running it, first assign values for the year, month, day, hour, minute, and second variables. Set the bar chart colors, too.

BARC INDEX 7

Y=25

O=12

D=31

H=23

M=59

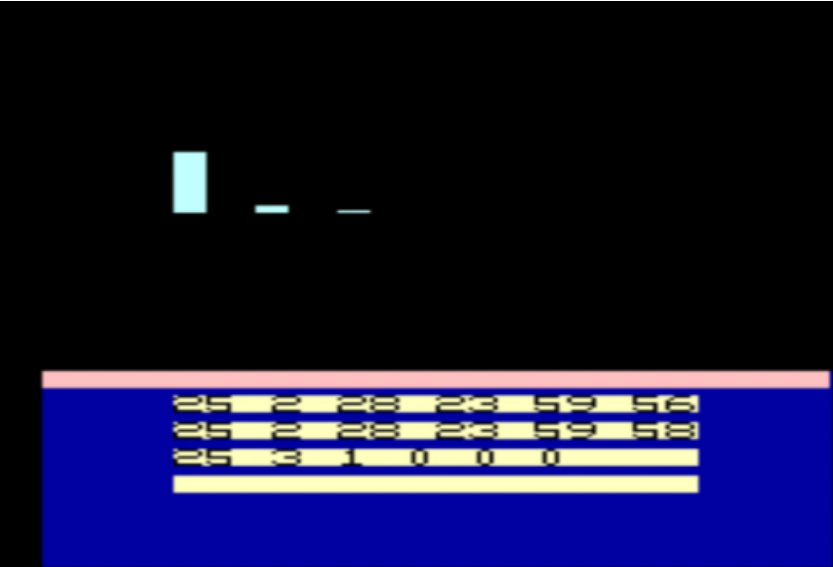
S=50

For example, these variables are for New Years Eve 2025, a ten second countdown to 2026.

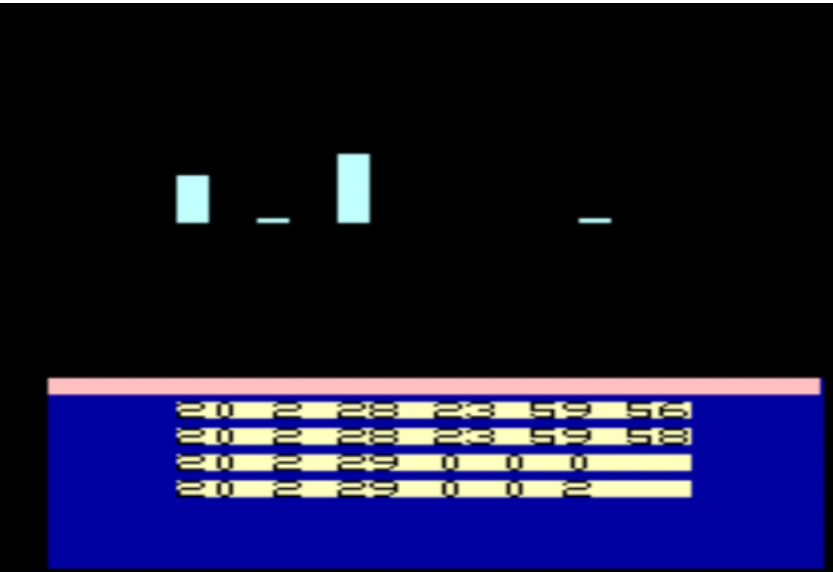
```

PROG CLOCK
WHIL 1
DO
    S=S+2
    IF S GE 60
    THEN S=0
        M=M+1
    ENDI
    IF M EQ 60
        THEN M=0
            H=H+1
    ENDI
    IF H EQ 24
    THEN H=0
        D=D+1
    ENDI
    IF (D EQ 30) AND (O EQ 2)
    THEN D=1
        O=3
    ENDI
    IF (D EQ 29) AND (O EQ 2) AND ((Y MOD 4) NE 0)
    THEN D=1
        O=3
    ENDI
    IF (D EQ 31) AND (+/(O EQ 4 6 8 9 11))
    THEN D=1
        O=O+1
    ENDI
    IF D EQ 32
    THEN D=1
        O=O+1
    ENDI
    IF O EQ 13
    THEN O=1
        Y=Y+1
    ENDI
    BARH Y,O,D,H,M,S
    Y,O,D,H,M,S
ENDW
ENDP

```



A non-leap year.



A leap year.

00

00

00

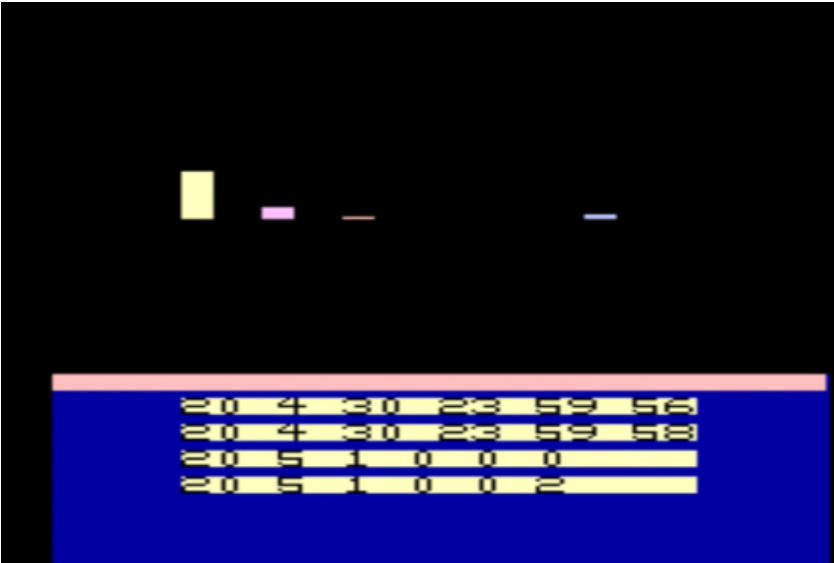
00

00 00 00 00 00 00 00 00

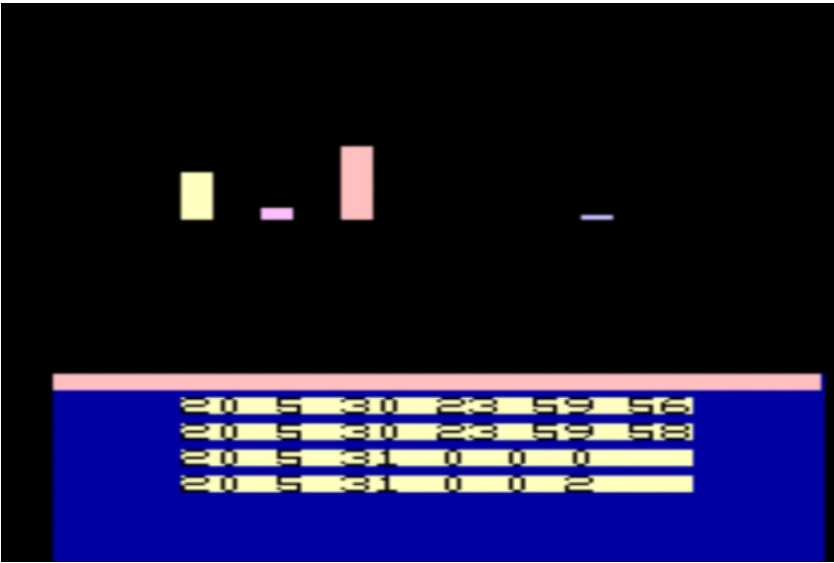
00 00 00 00 00 00 00 00

00 00 00 00 00 00 00 00

00 00 00 00 00 00 00 00



April has 30 days.



May has 31.



```

6
25 12 31 23 59 51
8

```



```

25 12 31 23 59 51
8
25 1 1 0 0 0

```


1

2

3

4

1

2

3

4

1

2

3

4

1

2

3

4

1

2

3

4

1

2

3

4

1

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1

2

3

4

1

2

3

4

1

2

3

4

1

2

3

4

1

2

3

4

Happy New Year!

Credits

All material from works authored or edited by David Ahl is in the public domain.

See <https://blog.adafruit.com/2022/06/16/david-ahl-places-all-his-classic-computing-publications-into-the-public-domain/>



The image is a screenshot of a Facebook post from David Ahl. At the top left is a circular profile picture of a man with a green hat. To its right is the name "David Ahl" and "8m · 🌐". At the top right are three dots. The main text of the post reads: "PUBLIC DOMAIN. This is a public notice that I am formally placing everything that I have written or edited into the Public Domain. That includes material that may or may not have a copyright issued to David Ahl, Creative Computing Press, Ahl Computing, Ideametrics, SBI, DEC, Military Vehicles, Ziff-Davis, or SwapMeetDave. My desire is that this material be used for educational and historical purposes and not for profit or personal gain of others. (I did this years ago, but someone wanted a public notice, so this is it.)" Below this text is a large light blue rectangular box with a black border. Inside the box, the words "PUBLIC DOMAIN" are at the top in large, bold, black capital letters. Below that, the text "This is a public notice that I am formally placing everything that I have written or edited (books, articles, programs, and tutorials) into the Public Domain." is written in bold black font. At the bottom left of the box, it says "David H. Ahl" and "June 15, 2022". To the right of this text is a white rectangular box containing a black handwritten signature that reads "David H Ahl".

David Ahl
8m · 🌐

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David H. Ahl
June 15, 2022

David H Ahl

The APL/S games in this book are collected here:

<https://github.com/jamescprice/21-APL-Games-and-One-Liners-For-Your-Umtech-VideoBrain/blob/main/21games.zip> – All the games in this book.

Preservation copies of the VideoBrain APL/S cartridge ROM are maintained by third-party retrocomputing archives for historical reference and research use. This publication includes APL/S program listings in printed form but does not include ROM images. For discussion see: <https://groups.io/g/Channel-F-and-VideoBrain/topic/101298602>

Documentation of The Computational Language APL/S:

<https://aplwiki.com/wiki/APL/S> Great technical description of the language at APL Wiki

<https://archive.org/details/byte-magazine-1979-12/page/n81/mode/2up> “APL/S: An Alternative” by Robert G. Brown BYTE magazine 12/1979

<https://archive.computerhistory.org/resources/access/text/2024/06/102804524-05-001-acc.pdf> – Two papers: "An Introduction to APL/S". Conference Proceedings of the Third West Coast Computer Faire” by Robert G. Brown p247 and “VideoBrain and the APL/S Language: First Pass at Everyman’s Computer” by Ted Haynes p246

<https://archive.org/details/apls-brochure/APLS-Brochure/> – Includes Lunar Lander game <https://forum.vcfed.org/index.php?threads/i-have-been-blessed-with-videobrain-documentation.80042/> - Links to zip file with great documentation and schematics

<https://forum.vcfed.org/index.php?threads/videobrain.71462/page-2> – Lots of documentation here!

Audio Discussion:

https://archive.org/details/camvchm_000053/camvchm_000053_t01_a_access.mp3 - "This is the recording of the session titled 'High level languages for micros,' and the following papers were presented: 'VideoBrain and the APL/S language: First pass at everyman's computer,' presented by Ted Haynes. 'An introduction to APL/S: A modern computational language for personal computing,' presented by Robert G. Brown."

<https://exhibits.stanford.edu/silicongenesis/catalog/nc497jv0418> – An interview with Albert Yu. 00:12:06 Discusses leaving Intel for Video Brain, where he developed microprocessors for use in consumer electronics. 00:17:52 Discusses leaving Video Brain in 1979 to sell home computers between the United States and China.

<https://randoc.wordpress.com/category/umtech-videobrain/> - Links to audio of conference talk

<https://www.orphanedgames.com/videobrain/>

More links:

http://hcvgm.org/Static/Manuals/VideoBrain/VB_Unit_Manual.pdf - System Manual with image of keyboard keys -

<https://randoc.wordpress.com/category/umtech-videobrain/> - A good discussion with many links

<https://www.atariprotos.com/othersystems/videobrain/cartridges/apls/apls.htm>

"The existence of APL/S has been speculated for years. More than one person has claimed to own the cartridge back in the day and it was mentioned in several advertisements, but no actual APL/S cartridge has ever been found. However in 2021 the first evidence of APL/S's existence turned up in the form of a manual in an eBay auction. Unfortunately the cartridge and box were nowhere to be seen. This all changed in 2023 when a complete copy of APL/S was finally located. Only 91 APL/S cartridges were ever made making it the rarest non-prototype VB cartridge."

<http://hcvgm.org/VideoBrain.html> - A keyboard diagram, machine specs

http://blog.kevtris.org/blogfiles/videobrain/videobrain_unwrapped.txt – A hardware deep-dive

<https://www.oldcomputers.net/videobrain.html> – Great images of system internals

https://www.ballyalley.com/articles_and_news/creative_computing_article.pdf – Two Creative Computing articles

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